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ABSTRACT

This paper describes and discusses three studies concerned with the representation of children's knowledge as revealed in the ways that children, ages 5 to 17, perform a scientific induction task. A variant of Piaget's balance scale prediction problem was chosen as the experimental task; a formal model for different levels of children's knowledge about how to do the task was constructed. Experiment I was conducted to assess the validity of this model. Experiment II examined some instructional issues and revealed some limitations of the initial representation. The results indicated that older and younger children who were initially classified by the model as having identical task-specific knowledge, showed a striking difference in responsiveness to instruction. This finding led to revising the original representation by analyzing the problem-by-problem performance of two children during a training sequence and using this information to formulate a detailed production system model of one child's knowledge. This model was then run as a computer simulation and a comparison of the computer results with the child's performance suggested that the initial encoding of the stimulus may account for the performance differences between older and younger children. Experiment III was conducted to test this encoding hypothesis. Finally, the types and levels of knowledge that might be important in instructional investigation were discussed. (Author/JMB)

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THE REPRESENTATION OF CHILDREN'S KNOWLEDGE

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THE REPRESENTATION OF CHILDREN'S KNOWLEDGE

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In this paper we will discuss two related issues. One issue concerns the ways that children from 5 to 17 years perform a scientific induction task. We will summarize a series of experiments designed to investigate questions about initial knowledge, instructional effectiveness, and individual differences in both initial performance and responsiveness to instruction. The second issue is methodological: its focus is not on what we can say about children's knowledge of a task, but rather on how we can say it. That is, the second issue we address is the representation of children's knowledge.

The two issues are related simply because the researcher's decision about how to represent knowledge plays a central role in guiding both the kind of theory that gets formulated and the kind of experiment that gets run. We have found this to be the case in our own studies, and we believe that it might be worthwhile to direct attention to some properties of different representations and criteria for choosing among them.

Our discussion will move back and forth between general conceptual issues and some very specific examples of both empirical techniques and theoretical statements. This will give the paper a rather complex organization, so we will sketch the structure at the outset:

I. From Behavioral to Cognitive Objectives.

First we describe the historical trend in instructional psychology that has made the representation of knowledge a central issue.

II. Some Criteria for Choosing a Representation.

Then we introduce criteria that we believe might be useful in choosing and evaluating different representations. In addition to a set of evaluative criteria, we list five central questions for research in developmental and instructional psychology.

III. The Balance Scale Task.

Next we introduce a specific task that has interesting psychological and instructional properties: a variant of Piaget's balance scale prediction problem. We present a formal model - using a particular representation - for different levels of

knowledge that children might have about how to do the task. The task provides the concrete reference for the remainder of our paper.

IV. Experiment 1: Assessing Initial Knowledge.

Having described the formal properties of the task, and some predictions about the performance of different aged children on it, we then describe our first experiment. Based upon the results of the experiment, we are able to evaluate the initial hypotheses, as well as to examine the merits and limitations of the representation in which the inital models are stated.

V. Experiment 2: Training on the Balance Scale Task

The initial representation and the associated experiment enable us to make certain predictions about the effects of an instructional sequence. In the second experiment we explore some instructional issues, and this in turn reveals some limitations of the initial representation. In particular, we find that older and younger children who are initially classified by our models as having identical task-specific knowledge, show a striking differential responsiveness to instruction. This presents a serious challenge to our initial representation of children's knowledge. It is clear that the initial formulation does not tell the whole story about differences in task specific knowledge.

VI. Revised representations for balance scale knowledge.

A revised representation of the knowledge required to perform at different levels is introduced. The representation is a production system, and some of the general properties of production systems are discussed. Then we present an analysis of the problem-by-problem performance of two children during a training sequence, and formulate a more detailed production system model of the knowledge of one of them. The model is actually run as a computer simulation and its results are compared with the child's performance. This fine grained analysis suggests that the initial encoding of the stimulus may be a crucial difference between older and younger children, and that this may account for the results of Experiment 2.

VII. Experiment 3: The encoding hypothesis

The encoding hypothesis states that differential responsiveness to training between 5 and 8 year old children is due to differences in the way that they encode the balance scale dimensions. The explanatory power of the hypothesis is tested in detail in Experiment 3.

VIII. Types of knowledge in the human information processing system.

We conclude with a brief discussion of the several types and levels of knowledge that might be important in instructional investigation. Different levels of aggregation of both model and data are obviously appropriate for different scientific questions. The direct and explicit consideration of some ways to represent knowledge provides useful guidelines for further empirical work.

From Behavioral to Cognitive Objectives

The goal of any instructional effort is the production of new knowledge in the learner. Over the last 15 years of instructional research there has been an increasing emphasis on stating such goals as clearly as possible. The trend was to move from an emphasis on simply describing educational means - the sequence of instructional activities - to a prior statement of the desired ends of instruction. The elaboration of behavioral objectives was perhaps the most extensive formalization of this trend(Mager, 1962). Behaviors were typically specified in great detail, although the underlying processes were not. However, even behavioral objectives have implicit in them an underlying cognitive theory: behavior is simply an observable indicator of underlying cognitive processes.

One well-known normative model for instruction (Glaser, 1968) stresses the need to determine the learner's initial state as well as the desired end state. In the original formulations of this approach, both initial and final learner states were described primarily in terms of tasks and subtasks arranged in a Gagne'-like hierarchy. There was little mention of how one might characterize the underlying psychological processes that acted upon them to produce the task behavior in question. As that approach has developed, however, it has focused increasingly upon such cognitive representations (see Resnick 1976, for a summary of this trend in the area of elementary mathematics instruction).

Perhaps the strongest statement of the desirability and feasibility of describing the learner in terms of internal psychological representations is Greeno's view of "cognitive objectives". Greeno(1976) argues that cognitive psychology has now developed powerful and flexible methods for the representation of knowledge. Using an example from instruction in elementary fractions, Greeno shows how two different views of the conceptual content of the subject matter can be represented explicitly by two quite distinct cognitive structures, which in turn lead to differential predictions about problem difficulty, problem solving strategies, and optimal procedures for instruction. Without such a representation, these predictions might have never been made.

This is essentially the same point stressed by Klahr & Wallace (1976) with respect to the need for explicit and precise models in cognitive development: "a theory of transition can be no better than the associated theory of what it is that is undergoing that transition." According to this view, the first step in the formulation of developmental theories is the creation of a precise model of the initial and final form of the cognitive process under investigation. Studies by Baylor & Gascon(1974), Young(1973), and Klahr & Wallace (1976) provide developmental models of this type.

In the area of adult problem solving, a similar emphasis on the importance of a good representation is made by Simon (1975). He provides an information processing analysis of adult performance on a simple task (the Tower of Hanoi puzzle) in order to demonstrate that several distinct strategies are all plausible models of task performance. Without an appropriate representational system, the precise distinctions among the strategies could not have been made.

Some Criteria for Choosing a Representation

What considerations might guide us in the choice of a representation? What kinds of representations are available, and what are their relative merits? Knowledge representation has become an important topic in the emerging field of "cognitive science" (Bobrow & Collins, 1975) and some initial attempts to address it can be found in Bobrow (1975), Becker (1975), Moore & Newell (1974), and Reddy & Newell (1974). These efforts constitute the first steps toward a full fledged theory of representation, and they have already yielded a reasonable set of dimensions with which to characterize different representations.

Although such taxonomic systems allow us to classify representations, they do not make any statements about their relative merits. Regardless of the final location of a representation along the dimensions of importance, the ultimate evaluation of the quality of a representation depends upon the set of questions being addressed.

We believe that in the area of instruction and development the important questions are:

Q1. What are the differences in knowledge that underlie different levels of task performance?

Q2. What are the alternative strategies that might result in any given level of task performance?

Q3. For a given level of performance, what is the optimal level of difficulty for an instructional sequence?

Q4. What are the critical features of an instructional sequence that enable it to have any effect?

Q5. When and why will two learners at the same initial performance level learn differently from the same instructional sequence?

Or, to summarize our concerns: what do children know about a task, how do they learn about it, and why do some know more and/or learn more than others?

Given this set of questions, there are four criteria that we believe to be most important in choosing a representation:

a. The representation must be sufficient to account for behavior. Thus, it must have a clear mapping onto the empirical base it is supposed to account for.

b. It should be amenable to multiple level analyses. That is, it should be easy to aggregate and disaggregate the grain of explanation. For the design of well controlled experiments or curriculum design, the representation will have to be stated in terms of averages across many subjects; it must be a modal form. For detailed study of individual strategies and component processes, it must be capable of disaggregation without drastic revision.

c. The representation should conform to the relevant properties of the human information processing system as determined by laboratory studies of human processing capacities.

d. The representation should have "developmental tractability"(Klahr & Wallace, 1970). It should allow us to state both early and later forms of competence and provide an easy interpretation of each model as both a precursor and successor of other models in a developmental sequence (see Resnick, 1976, for a similar viewpoint).

The Balance Scale Task

The type of balance scale used throughout our investigation consisted of a two-arm balance, with several pegs located at equal intervals along each arm. Small circular disks, all of equal weight, were placed on the pegs in various configurations (as shown in Table 1), while the balance was prevented from tipping. The subjects' basic task was to predict the direction in which the balance scale would move if it were allowed to. In order to answer some of the questions listed above, several variations on this basic theme were introduced. These included asking children to explain their predictions, allowing the scale to move to its equilibrium position(thus providing feedback about the accuracy of the predictions), observing an experimenter-controlled series of configurations and their effects, constructing one's own configurations, and reconstructing initial configurations from memory (the details of these experiments are presented in Siegler, 1976).

The basic physical concept that underlies the operation of the balance scale is torque: the scale will rotate in the direction of the greater of the two torques acting on its arms. The total torque on each arm is determined by summing the individual torques produced by the weights on the pegs, and the individual torques are in turn computed by multiplying each weight by its distance from the fulcrum. Since the pegs are at equal intervals from the fulcrum, and the weights are all equal, a simpler calculation is possible. It consists of computing the sum of the products of number of weights on a peg times the ordinal position of the peg from the fulcrum. This is done for each side, and the side with the greater sum of products is the side that will go down (if they are equal, the scale will balance).

The components of this knowledge are acquired over a remarkably long span of experience and education; even 5-year olds often know that balances such as teeter-totters tend to fall toward the side with more weight, while many 16-year-olds do not know the appropriate arithmetic computations for determining the balance's behavior (Jackson, 1965; Lee, 1971; Lovell, 1961). It even seems likely that most college educated adults could not easily state the physical principles that underlie the sum-of-products algorithm. Furthermore, for many configurations, there are shortcuts that eliminate the need to do any arithmetic computation (e.g.,identical configurations on each arm will balance; if both weight and distance are greater on one side, that side will go down).

Note that the balance scale task shares a common property of many scientific problems: the universal rule for generating correct predictions is easy to describe, and once known, it is easily remembered and executed. However, the formulation of the rule - either by induction from empirical examples or by deduction from general physical principles - is quite difficult.

A representation of children's knowledge about the balance scale

The knowledge that children at different levels of performance have about this task can be represented in the form of a binary decision tree, as shown in Figure 1. The model of mature knowledge (Model IV) was suggested by a rational task analysis of balance-scale problems (cf. Resnick,1976); the models of less sophisticated knowledge (Models I - III) were derived from the empirical results of Inhelder and Piaget(1958) and Lee (1971), and from our own pilot studies. A child using Model I attends only to the number of weights on each side: if they are the same, the child predicts balance, otherwise he predicts that the side with the greater weight will go down. For a Model II child, a difference in weight still dominates, but if weight is equal, then a difference in distance is sought. If it exists, the greater distance determines which side will go down, otherwise the prediction is balance. A child using Model III tests both weight and distance in all cases. If both are equal, the child predicts balance; if only one is equal, then the other one determines the outcome; if they are both unequal, but on the same side with respect to their inequality,then that side is predicted to go down. However, in a situation in which one side has the greater weight, while the other has the greater distance, a Model III child, although recognizing the conflict, does not have a consistent way to resolve it. This child simply "muddles through" by making a random prediction. Model IV represents "mature" knowledge of the task: since it includes the sum-of-products calculation, children using it will always make the correct prediction. Note, however, that if they can base their prediction on simpler tests, they will do so.

Figure 1 about here

Assessing the accuracy of the representations

We can determine which - if any - of these four models accurately characterizes a child's knowledge about the balance scale task by examining his pattern of predictions for six types of problems (see Table 1 for an example of each type):

1) Balance problems, with the same configuration of weights on pegs on each side of the balance.

2) Weight problems, with unequal amounts of weight equidistant from the fulcrum.

3) Distance problems, with equal amounts of weight different distances from the fulcrum.

4) Conflict-weight problems, with more weight on one side and "more distance" (i.e. occupied pegs further from the fulcrum) on the other, and the configuration such that the side with more weight goes down.

5) Conflict-distance problems, similar to conflict- weight, except that the side with more distance goes down.

6) Conflict-balance problems, like other conflict problems, except that the scale remains balanced.

Table 1 about here

Children whose knowledge corresponded to different models would display dramatically different patterns of predictions on the six types of problems just listed. Those using Model I would consistently make correct predictions on balance, weight, and conflict-weight problems, and they would never be correct on the other three problem types. Children using Model II would behave similarly to those using Model I on five of the six problem types, but they would correctly solve distance problems. Those following Model III would consistently make accurate predictions on weight, balance, and distance problems, and would perform at a roughly chance level on all conflict tasks. Those using Model IV would solve all problems of all types.

To the extent that there is a correlation between age and the level of the model which best represents a child's knowledge, there should be clear developmental patterns for each problem type. The most interesting is the predicted decrement in performance on conflict weight problems Children using Models I or II will get these problems right even though they do not see them as conflict problems, whereas children using Model III will attend to the conflicting cues of weight and distance, but they will have to muddle through, and their resulting predictions will be at a chance level of performance. Another prediction, shown in Table 1, is that distance problems should show a dramatic improvement with age. The youngest subjects - using Model I - will get them all wrong, while children using Models II, III, or IV will get virtually none wrong. By a similar logic each of the problem types yields a predicted developmental course, the results of which are shown in Table 1 (see Siegler, 1976, for a complete analysis).

Experiment 1: Assessing Initial Knowledge

The purpose of Experiment 1 was to assess the validity of the foregoing analysis for a group of children spanning a wide age range

Method

Subjects were 120 female students from a private school in Pittsburgh.

Fifteen students from each of 8 grade levels were grouped as shown at the top of Table 2.

Materials included a wooden balance scale, 10 different-colored metal weights, and 2 wood blocks. The balance scale's arm was 32 inches long, with 4 pegs on each side of the fulcrum. The first peg on each side was three inches from the fulcrum and each subsequent peg was three inches from the peg before it. The arm could swing freely from the point of attachment to the fulcrum, four inches above the fulcrum's base. Each metal weight weighed 1.4 ounces, measured 1 inch in diameter, and had a hole in its middle so that it would fit on the pegs; as many as 6 weights could be placed on any one peg. The two blocks of wood, each four and one-half inches high, could be placed under the arm of the balance scale to prevent it from moving regardless of the configuration of the metal weights on the pegs.

Children's knowledge was assessed through a 30 item test. On each problem the experimenter started with an empty balance, the arms of which were supported by the two wooden blocks. Then the metal weights were placed on the pegs on the two sides of the balance scale, and the child was asked to predict which side would go down or whether the scale would balance if the two wooden blocks, underneath the arms of the balance, were not there. Among the 30 items were 4 balance, 4 weight, 4 distance, 6 conflict-weight, 6 conflict-distance, and 6 conflict-balance tasks of the types shown in Table 1.

Children were tested individually in a quiet room in their school. The experimenter's initial instructions were:

> "Today we are going to play with this balance scale. The balance scale has these pieces of wood that are all the same distance from each other (pointing to the pegs) and these pieces of metal that all weigh the same."

At this point the children were encouraged to hold the weights to see that they weighed the same amount and to observe the equal distances between adjacent pegs.

Children's knowledge was then assessed by presenting them with the 30 problems described above. The problems were introduced with the following instructions:

> Let's see what you know about the balance scale. I'll put the weights on the pegs in different ways and you tell me whether this side would go down or this side would go down or they would both stay like they are now if I took the wood blocks away. The balance scale won't actually move, but you tell me how the scale would go if the pieces of wood were not there.

Following this test, children were asked to explain their responses. Children spent between 15 and 30 minutes on the entire task.

Table 2 about here

Results

The percent correct predictions for each problem type by each age group is shown in table 2. A 4(age) by 6(problem type) ANOVA revealed that both main effects and their interaction were significant ($p < .001$). Note that the developmental patterns are very close to those predicted in Table 1. In particular there is a dramatic improvement in distance problems and a decrement in conflict-weight problems. The conflict-weight problems never did show an upturn, although performance appears to have leveled off for the older age groups.

Not shown in Table 2 is the substantial consistency that existed in performance on items within each problem type. Only on conflict-weight problems did accurate prediction decrease with age, and within this category such decrements occurred on all six problems. The magnitude of the improvement over age on the 4 distance problems was unmatched by that on any of the 26 other items. On all eight of the balance and weight items, but on no other tasks, was the developmental trend minimal.

With one class of exceptions, the four models make exact predictions about which of the three possible responses (left down, right down, balance) the subject will make on each one of the 30 problems (the exception class contains the 18 conflict problems for Model III; here the prediction is a lack of consistency, i.e. essentially chance responding). Thus, we can compare the response pattern of each child to the predicted patterns for each of the models, and classify the child according to which, if any rule she was using in making her predictions. Using a very strict criterion - one that would misclassify a random responder less than one time in a billion for rules I,II, or IV, or less than once in ten thousand for rule III, we were able to classify 107 of the 120 children. The results are shown in Table 3.

Table 3 about here

Children's explanations were also used to determine which model the child was using. The criteria for classifying according to explanations were derived from a literal interpretation of the models. Altogether, 117 of the 120 children's explanations fit one of the four models. As shown in Table 4, the two classifications - one derived from children's predictions, the other from their explanations - were highly correlated ($r = .89$, $p < .001$). All of the 23 children judged to be using Model I by the predictions data were judged as using Model I by the explanations criterion and all 8 of the children classified as using Model IV on the predictions measure - and only those eight - were classified as using Model IV on the explanations measure as well. On the other hand, many children were classified as using Model II by the predictions measure who were placed in Model III by the explanations measure.

Table 4 about here

One interpretation of this discrepancy between the explanations and predictions

criteria is that there were some children who used Model III tests, but consistently resolved the conflict by relying on the weight cue. Further evidence that children knew more about the balance-scale than is revealed by the predictions classification comes from an analysis of the content of their explanations. Fully one-third of the children advancing Model III explanations cited the ratio property of conflict-balance problems (e.g., one on the third peg equals three on the first peg), but not the composition rule necessary for a Model IV placement.

Evaluation of decision-tree representations

How well do the decision trees used in Figure 1 represent children's knowledge on the balance scale task? It appears to fare well on the first and last of the four criteria listed earlier. It is clearly adequate to account for the predictions data. The problem type by model analysis provided an exhaustive an unambiguous mapping between behavior and theory. The formal relationship between the models is one of strict inclusion: Model I tests are included in Model II, etc. This logical structure predicts an invariant developmental sequence (although we could not test this directly in a cross-sectional study).

On the other two criteria - multiple level analysis and integration of psychological parameters - the merits of the representation are less clear. The data can be aggregated and disaggregated between group and individual levels, but only two kinds of analyses -- prediction and explanation -- are described. Additionally, no statements about psychological - as opposed to logical - properties of the knowledge required to do the task have yet been advanced.

Another orientation from which to evaluate the representation is to ask how well it answers the 5 questions about instruction and development that were listed above. Thusfar, it has only answered Q1: the difference between high and low performers is represented by differences among the four models. The models are silent on Q2, which addresses the issue of alternative paths to the same performance. This inadequacy was most noticeable in our discussion of the idiosyncracies that are masked by the "muddle through" category on Model III. Since the models do not have any representation for their own induction, they are unable to say anything about Q4, which asks about critical features of the instructional sequence. However, the models do suggest some straightfoward ways to empirically investigate Q3 (how difficult should an instructional sequence be?), and they imply that there should be no differences in responsiveness to instruction, thus providing an assertion that refutes the premise of Q5. In Experiment 2, we addressed these issues suggested by Q3 and Q5.

Experiment 2: Training on the Balance Scale Task

In the second experiment, five- and eight-year olds were equated for performing at a level not beyond Model I. Then they were provided with experience on either distance or conflict problems, or with one of two control procedures.

Distance problem experience focused on the type of problems solvable by Rule II but not by Rule I; it thus was geared one step above the learners' initial level. Conflict problem experience, emphasizing problems not understood even qualitatively until Rule III, was intended to be two or more steps advanced. According to Piagetian theory, the fit between a child's existing knowledge and the new information presented is a critical determinant of when, how much, and what kind of learning will occur (Piaget, 1971). Support for this view has been found by Turiel (1966) and Blatt (1971) in the area of moral development, and by Kuhn (1972) in class-inclusion training. Therefore, we predicted that our Model I children would benefit from distance problems, while they would learn little, if anything, from conflict problems.

As we already noted, there is nothing in the models that would predict differential responsivity to instruction of older and younger children. But both intuition and empirical evidence support the notion that older children are more adept than younger ones at mastering many novel problems on which task-specific knowledge is equally lacking (cf. Siegler & Liebert, 1974, 1975; Siegler, 1975). Thus we had no clear grounds on which to base a prediction about age differences in response to our training sequences.

Method

Experiment 2 included three segments: pretest, experience, and posttest.

Pretest. The pretest consisted of eight items: two weight, two distance, two conflict-weight, and two conflict-distance. The tasks and apparatus were similar to those used in the posttest in Experiment 1; on each trial, the child was shown a configuration and asked to predict which of the three possible outcomes would occur if the wood blocks were removed. There was no feedback during the pretest.

Experience. All experiential conditions except the bias control (see below) included 16 trials on which children were presented a randomized sequence of various types of balance scale problems. Children were asked to predict what would happen and why they thought so; then the wood blocks supporting the scale were removed so that the prediction was confirmed or disconfirmed. After a 10 second interval the weights were removed and placed on the scale in a different arrangement.

Conflict problem experience involved presentation of 6 conflict-weight, 6 conflict-distance, 1 distance, 2 balance, and 1 weight problem. Distance problem experience included 12 distance, 2 balance, and 2 weight problems. Thus, each experiential condition included 12 problems of the type being emphasized; the additional 4 problems of other types were intended to prevent children from acquiring strategies too narrowly suited to the demands of the majority of items.

Within the control condition there were two sub-groups: the exposure control and the bias control. The exposure condition was designed to control for the possibility that any experience with the balance scale could improve performance; children in this condition were presented a sequence composed of 14 weight and 2 balance items that would familiarize them with the balance scale's workings but would

not directly engender knowledge of Models II or III. However, this control procedure might itself bias children toward a greater reliance on Model I than if they had been left untutored. Therefore, a bias control was included in which children simply received the pretest and posttest. Within each age group's control condition, one-half of the children were assigned to the exposure control and one-half to the bias control.

Posttest. The posttest included a randomly ordered, no-feedback presentation of 24 items, 4 each of balance, weight, distance, conflict-weight, conflict-distance, and conflict-balance types. The pretest took approximately 10 minutes, the experience 25 minutes, and the posttest 15 minutes. Eight-year-olds were given the three parts in succession; five-year-olds were given the pretest one day and the experience and posttest in a second session within the next 48 hours.

Participants. Pretests were given to 109 children, 56 kindergarteners (five-year-olds) and 53 third graders (eight-year-olds), attending a middle class school in suburban Pittsburgh. To equate the initial knowledge of participants, children whose responses were consistent with the distance cue on both distance tasks or on more than two of the six distance and conflict items were excluded from further participation in the experiment. This eliminated 21 children--1 male and 1 female five-year-olds, 8 male and 11 female eight-year-olds. An additional 28 children--17 female and 7 male five-year-olds, and 4 female eight-year-olds--were excluded randomly from experiential and posttest phases in order to equate age and sex characteristics of the age and treatment groups. These children differed in no systematic way from their peers who did participate. Finally, the remaining 60 children, 30 five-year-olds and 30 eight-year-olds, were randomly assigned within age and sex to the three treatment groups. All groups had equal numbers of males and females except for the eight-year-old control group that included 4 boys and 6 girls. The mean CA of kindergarteners was 70 months (range = 66-75 months), while the mean CA of third graders was 106 months (range = 101-117 months). The experimenter, a 22-year-old female research assistant,served for all children.

Results

Responses to the 24 item posttest were classified according to a scheme similar to the one used in Experiment 1. (There were no differences between the two control groups, so all control data has been aggregated over both of them). As shown in Table 5, 45 of the 60 children behaved according to the models: 21 using Model I, 17 using Model II, and 7 using Model III. A Chi Square Test indicated that significant differences were present in the type of rules used by children in the six age by experience groups ($X2 = 45.54$, $df = 1$, $p < .001$). More specific analyses revealed that five-year-olds more often used Model I and eight-year-olds more often Models II or III ($X2 = 12.91$, $df = 1$, $p < .001$), and that children exposed to the control procedure more often used Model I while those exposed to conflict or to distance problems more often used Model II or III ($X2 = 13.20$, $df = 1$, $p < .001$).

An interactive relationship between type of experience and age was also apparent. Fisher Exact tests indicated that among five-year-olds, experience with distance problems led to more adoptions of Models II and III than did experience with

conflict problems or the control conditions ($p < .01$). As can be seen in Table 5, the effect was almost exclusively to promote attainment of Model II; no condition led to many children attaining Model III. Among the eight-year-olds, however, both distance and conflict problem experience led to more adoptions of Models II and III than did the control procedures ($p < .001$) and conflict problem experience led to greater use of Model III than did the distance problems and control conditions ($p < .01$).

Table 5 about here

In summary then, Table 5 shows us that both age groups can learn from training that is only one level beyond their current level (i.e., distance training). However, given training that is two levels beyond (i.e conflict training), the 5-year-old children learned nothing, while the 8-year-olds benefitted substantially. Thus it is clear that older and younger children derived different lessons from the same experience, even when they had identical initial predictive knowledge about the task.

Revised Representations for Balance Scale Knowledge

These empirical results raise questions that reveal some of the limitations of the decision tree representation used thusfar to represent children's knowledge of balance scale tasks. Since the four models purport to represent all of what a child knows about the task, they predict that children classified according to one of the models should be identical on all task related performance, including learning about the task. Thus, they predict that the differential responsiveness to experience with conflict problems that we observed between 5's and 8's should not have occurred. Of course, the models make this prediction by default,since they have no representation of the learning process as such. That is, they contain no representation of the way that positive and negative information obtained during the training sequence is treated, nor about the ways in which the models might undergo transformation from one level to the next.

Another limitation of the representation is that it allows no way to describe the many different means utilized by our subjects to arrive at the same end. We have already alluded to this in our discussion of the Model III explanations data, and now it is time to address it directly.

We need a representation that can account for not only the logical form of the decision rules used to make predictions, but also the psychological properties of the rules. That is, we need a representation that enables us to clearly indicate the perceptual and mnemonic demands of actually using the decision rules. In this section we will introduce such a representation for childrens' knowledge about this task, and we will present examples of the kinds of questions the representation enables us to ask. Then, in the next section, we will describe an experiment that provides some answers to these questions.

A production system representation

In Figure 2 we have restated the four models of Figure 1 as production systems (see Newell, 1973 for an extensive introduction, and Klahr, 1976b, for some examples from cognitive development.) A production system consists of a set of rules - called productions - written in the form of condition - action pairs, the conditions are symbolic expressions for elements of knowledge that might be present at some instant. A production system operates via a recognize - act cycle. During the recognition cycle, all the condition sides of all the productions are compared with the current contents of the knowledge state. The knowledge state can be viewed as short term memory, or the currently activated portion of long term memory, or simply as the current state of awareness of the system. The productions whose conditions are true of the knowledge state are placed into the conflict set, a conflict resolution principle is applied, and one production fires. The act cycle executes the actions that are associated with the fired production. Then the next recognition cycle commences.

Thus the conditions are tests on the moomentary state of short term memory (STM). A sequence of condition elements on the left side of a production is interpreted as a test for the simultaneous existence of the conjunction of the individual knowledge elements. If, for a given production, all the condition elements happen to be true at some instant, we say that the production is "satisfied". If only one production is satisfied, then it "fires": the actions associated with it, written to the right of the arrow (see Figure 2) are taken. These actions can modify the knowledge state by adding, deleting, or changing existing elements in it, or they can correspond to interactions with the environment - either perceptual or motor.

If more than one production is satisfied at a given moment, then the system needs to invoke some conflict resolution principle. In the systems shown here all conflicts are assumed to be resolved such that special cases have priority over general cases. For example, suppose that the two productions in the conflict set are:

P.ONE:(a b --> c d)
P.TWO:(b --> f g).

P.ONE is a special case of P.TWO, since P.TWO is satisfied whenever element "b" is in the knowledge state, but P.ONE is only satisfied if "b" plus additional information - in this case "a" - is also in the knowledge state. Thus, P.ONE will be chosen to fire. P.TWO will fire only when b, but not a, is true of the knowledge state. (Extensive discussions of production systems can be found in Newell, 1972, Newell & McDermott, and Rychener, 1976).

Figure 2 about here

Consider, for example, Model II in Figure 2. It is a production system consisting of three productions. The condition elements in this system are all tests for sameness or difference in weight or distance. The actions all refer to behavioral responses.

None of the models in Figure 2 contain a representation for any finer grain knowledge, such as the actual amount of weight or distance, or the means used to encode that information. Nor is there any explicit representation of how the system actually produces the final verbal output. It is simply assumed that the system has access to encoded representations of the relational information stated in the conditions. We will return below to further consideration of the way that this information becomes available to the system. Returning to Model II, notice that on any recognize cycle, only one production will fire. If the weights are unequal, then P2 will fire; if the weights are equal and the distances are not,then both P1 and P3 will be satisfied, but since P3 is a special case of P1, the conflict resolution principle will choose P3 to fire; finally, if both weights and distances are equal, then only P1 will be satisfied and it will fire.

The production system versions of the other three models are also shown in Figure 2. [The numbers attached to the productions (e.g. P1, P2, etc.) are not supposed to have any psychological meaning. They serve simply as labels for the reader; note that a production maintains its label across the four models.]

We can compare the four models to determine the task facing a transition model. At the level of productions the requisite modifications are straightfoward: a transition from Model I to Model II requires the addition of P3; from II to III, the addition of P4 and P5; and from III to IV, the addition of P6 and P7, and the modification of P4 to P4A (this modification changes the action side from random muddling through to "get.torque").

We can compare the four models at a finer level of analysis by looking at the implicit requirements for encoding and comparing the important quantities in the environment. Model I tests for sameness or difference in weight. Thus it requires an encoding process that either directly encodes relative weight, or encodes an absolute amount of each and then inputs those representations into a comparison process. Whatever the form of the comparison process, it must be able to produce not only a same-or-different symbol, but if there is a difference, it must be able to keep track of which side is greater. Model II requires the additional capacity to make these decisions about distance as well as weight. This might constitute a completely separate encoding and comparison system for distance representations, or it might be the same system except for the interface with the environment.

Model III needs no additional operators at this level. Thus it differs from II only in the way it utilizes information that is already accessible to Model II. Model IV requires a much more powerful set of quantitative operators than any of the preceding models. In order to determine relative torque, it must first determine the absolute torque on each side of the scale, and this in turn requires exact numerical representation of weight and distance. In addition, the torque computation would require access to the necessary arithmetic production systems to actually do the sum of products calculations.

Although we have compared the four models at two distinct levels - productions and operators - the levels are not really that easily separated. Missing from these models are a set of productions which would indicate the

interdependence: productions that explicitly determine which encoding the system will make. That is, in these models, there are almost no productions of the form: (want to compare weights) --> (attend to stimulus and notice weight). The sole exception to this occurs in P4A in Model IV. When this model is confronted with a non-conflict problem, either P1, P2, P3, or P5 will fire on the first recognize cycle. However, if it is a conflict problem, then P4A fires, and the system attempts to "get torque". The result of this unmodeled action, as described above, would be to produce a knowledge element that could satisfy either P6 or P7 on the next recognize cycle.

Evaluation of the Production System Representation

Each of the four production system models in Figure 2 makes precisely the same prediction as its counterpart in the decision tree representation of Figure 1. Thus, on the first of the evaluative criteria listed above -- accounting for behavior -- the production system model fares as well as the decision tree model. With respect to the second criterion -- multiple level analysis -- and the fourth -- developmental tractability -- the production systems have some advantages over the decision trees. They make explicit the requirements for both the encoding operations and the rules (i.e. productions) that utilize the symbolic elements produced by the operators. They also clarify the developmental differences between models in terms of these two kinds of entities. Although the production systems in Figure 2 are modal forms, we will demonstrate below the ease with which they can be recast in order to account for a single subject's performance.

The major advantage of the production system representation lies in its integration of general psychological principles -- the third of our evaluative criteria. Production systems of the type used here incorporate a theory of the control structure and general representation that underlies a broad range of human problem solving ability (Newell & Simon, 1972). As Newell (1973) puts it:

> The production system itself has become the carrier of the basic psychological assumptions -- the system architecture of ...[the production system] is taken to be the system architecture of the human information processing system (516).

Thus, models written in this form can be viewed as variants within a general psychological theory, and to the extent that such a general theory is consistent with the empirical results from experimental psychology, then these models are also consistent with them.

With respect to the five questions listed earlier, the production systems have enabled us to be very explicit about Q1 (differences that underlie performance), and in particular about the important role of encoding operators. They have indicated some potential sources of variation for each level of performance (Q2), although since they are written as modal types, this is merely suggestive at this point. Similar comparisons of the relative efficacy of the two forms of representations for answering the other three questions yield the same result. Thus, while the new representation does not

provide much of an advantage over the old for understanding the results of Experiment 2, it does provide some guidance about where to look for an explanation: in the encoding of the stimulus.

In order to model the conditions under which one or another aspects of the stimulus are attended to and encoded, we would need to augment the models in Figure 2 with productions like P4A. These productions would transform the models from simple discrimination nets, into active problem solvers, and they would enable us to make predictions about such things as eye-movements and solution latencies for different classes of problems. However, before we can make such an extension, we must first determine the varieties of possible encoding schemes that subjects are actually using. As a first step in that direction, we undertook a detailed examination of the problem by problem protocols of a few children in a training sequence.

Protocol analysis

Several children, ranging in age from 5 to 10 years were unsystematically selected to be run individually in a conflict training sequence. They were given instructions about the balance scale and about the fact that there were rules underlying the balance-scale's behavior that they could discover if they "watched carefully and thought about it". In addition, following their prediction on each trial, they were asked to state their reasons for the prediction. Then the blocks were removed, the children observed the scale's movement and if they were incorrect, they were again asked "Why do you think that happenned?"

These entire sessions were video-taped, and then all the verbal comments, as well as major physical activities were transcribed into the form shown in Appendix A. At the beginning of each problem, there is an indication of the problem number, the configuration, and the elapsed time (in minutes and seconds) since the start of the session. Problem numbers T1, T3, etc., correspond to items from the training sequence, and problem numbers E7, E8, etc, (see lines 11000, and 14400) are from an exploratory session which followed the training sequence. In the exploratory session, the children were encouraged to build interesting problems,or to explain to the experimenter what kinds of problems would achieve certain outcomes. The problem configuration is indicated by a numerical code that is a near-pictorial representation of the problem. In T1 (line 100) the code 0001/2000 indicates one weight on the first peg (from the fulcrum) on the left side, and two weights on the first peg on the right side. In T3 (line 1900), the code 0100/1000 indicates a single weight on the third peg on the left, and a single weight on the first peg on the right.

Excerpts from the protocol of Anna, a five year old female, are shown in Appendix A. The protocol provides a rich data source from which to select "observations". However, in this discussion we will focus only on those aspects that indicate the kind of encoding of distance and weight that Anna appears to use.

Anna was first given the standard instructions and pretest described earlier. Her response pattern did not conform to any of the four models. However, if

Model I were modified such that heavy things went up instead of down, then she was a perfect Model I subject. The first problem in the training sequence confirms this interpretation (lines 100 - 1700). Anna knows which side has more weight, but her prediction is based upon the assumption that more weight goes up. However, when confronted with the contrary evidence, she changes the "sign" of the correlation between weight and direction of tipping. This single feedback trial was sufficient: for the remainder of this half hour session, she never again errs in her understanding of the direction of the effect of weight differences. As we will see, the correct encoding of distance and its effect required a much longer series of trials.

The second training problem (not shown) was a balance problem, so T3 (0100/1000) was the first instance in which Anna received feedback indicating that equality of weight is not a reliable predictor. Her own verbalization of the problem captures her puzzlement. "Well why are they both the same thing [same weight] and one's up and one's down?"(line 3000)

Another distance problem followed immediately (T4: 0020/0020), and Anna's first response is to say balance, but she quickly corrects herself, having detected the distance difference. Her encoding of distance is correct in that it is based on the fulcrum, rather than the endpoints, as the zero reference point (lines 4100 - 4200). However she incorrectly associates greater distance with the side that goes up rather than the opposite, in the same way that she initally had the sign wrong for weight effects. This is her first attempt to utilize distance information, and she gets negative feedback. At this point she might abandon distance as a useful cue, or she might - as she did with weight - simply change the sign of the relation. As we will see, she does neither.

T5 was a complex distance problem (0101/1100), and T6 (0102/2010) a balance problem, niether one of which yielded a useful protocol. In T7 (0200/2000) we return to a distance problem. It is clear from the protocol that Anna is still attempting to use distance (lines 9000 - 10600). She still encodes direction of distance from the fulcrum correctly, but she has not changed her erroneous assumption about the effect of this difference. Note also that she has not yet made any statement about absolute amount of distance: all her statements are about relative distance.

In order to focus on the issue of distance encoding, we skip over about 15 minutes of conflict training in which the problems were mainly complex conflict weight and conflict distance (i.e. two or more pegs occupied on each side) from which no clear pattern emerged. We pick up the protocol again in an excerpt from the exploratory phase in which Anna was allowed to construct problems according to various experimenter requests or hints. In E7 (lines 11000 - 14100), she has been asked to construct some problems such that she will not be quite sure what the result will be. In general, Anna does no such thing, and instead tends to construct problems about which she is very confident. Thus, her initial configuration is 0003/0004, a problem in which both weight and distance indicate that the right side will down. Then the experimenter modifies it to a distance problem (0004/0004), and Anna apparently forgets all about distance differences, reverting to a Model I prediction of "balance" (lines 11700 - 13000). With a little prompting from the

experimenter (lines 13200 - 13700), she invokes a (post hoc) distance explanation (lines 13800 - 13900). Notice that the distance description is not just a relative judgement, but instead is stated in terms of two absolute (albeit approximate) quantities.

It appears that, even after almost 30 minutes of experience with the balance scale, Anna knows that distance is an important factor, but she has not yet developed a reliable rule about the effect of distance differences. Then, over the next two minute period, she begins to demonstrate a stabilizing grasp of this concept. First she creates a balance problem and makes the correct prediction (lines 14400 - 15600). Then a new experimenter enters, and feigning ignorance, asks how the scale works. Anna creates (0003/0003) and predicts correctly, and for the right reasons (lines 16500 - 17400). Then, at the experimenter's request, she correctly creates a balance problem (0003/3000). It is interesting that she does this in the "easiest" way, given the configuration from which she was starting, but it is also the case that this is the same balance configuration that was used in the preceding problem. Then she creates a distance problem such that the scale tips in a desired direction (18700 - 19100) and gives the correct explanation, and finally, she initiates yet another balance problem, one unlike any she has ever seen before (3000/0003).

Recall that this protocol analysis was undertaken after a discussion of the production system representation of knowledge about the balance scale (Figure 2). In that representation, we tried to emphasize the differences between the encoding of information about the environment (the undefined operators) and the combination rules [cf. Gelman's (1972 a,b) operator-estimator distinction, and Klahr & Wallace, 1973, operator-rule dichotomies]. for acting on that information (the productions). The protocols tell us something about the nature of the representations that are being used by the child, and hence something about the encoding operators that produce them. It is clear that Anna extracts information from the training series that will enable her to improve both the encoding operators and the combination rules. With respect to weight, she has no difficulty in formulating an appropriate encoding based on counting the number of weights. Although there is an initial error with respect to the relation between weight differences and the direction of the scale, this is quickly corrected and remains stable for the rest of the session.

Distance encoding follows quite a different course. Initially it is ignored. Then differences in distance are noted, but their effect is quite unstable in the face of negative feedback, and as we saw, they are occasionally ignored well into the training sequence. However, it appears that by the very end of the exploratory trials, an appropriate encoding of distance, and a concomitantly appropriate rule for utilizing it (at least on distance problems) has been formulated.

Learning about the balance scale then, would seem to require much more than is suggested by a comparison of adjacent models in Figure 1. The production system representation of Figure 2 has enabled us to make explicit the difference between encoding operators and decision rules, and it has guided our search for instances of both of these kinds of learning in the protocol. The analysis suggested that there is a point in the development of knowledge about this task

during which the dimensions may be encoded in idiosyncratically incorrect ways, and that the form of the encoding may depend upon trial to trial feedback. In the next section we will introduce a model that attempts to capture these phenomena for an individual subject.

Revised production system for a Model III child.

Thusfar, the production system representation has been used only to suggest some of the complexities of learning about the task. In this section we will work toward the creation of a production system model of a single child's behavior during a training sequence. The representation will be more than suggestive, for it will be specific enough to run as a computer simulation. The simulation will serve two purposes. First, it will demonstrate the sufficiency of the model to account for the data it purports to explain. Second, the particular simulation language in which the model is stated is based upon, and incorporates in its structure, very specific assumptions about the nature of the human information processing system. Thus, the model to be described here is a particular instance of a much broader theory of human problem solving.

Our subject - Pam - was a female second-grader, age 7 years,11 months. Her performance on an 8-item pretest and a 16-item training series is shown in Table 6. In Table 6, each row corresponds to a problem. The columns indicate, respectively, problem number, problem configuration, problem type (Distance, Balance, Conflict-Weight, Weight, etc.), Pam's response (Left or Right down, Balance), feedback from the scale (if the subject's prediction was inconsistent with what the scale did, it is indicated by a "-"), predictions from three of the previously described models (IV, II, and I), and finally, two columns corresponding to the model to be described in this section. The first of these columns - III-A - contains the model's prediction, and the second contains the value of a variable criterion that is used to make the prediction. For example, Problem 7 has 3 weights on the first peg on the left and 2 weights on the third peg on the right; it is a conflict-distance problem. Pam predicted that the left side would go down, but as Model IV (which is always correct) predicted, the right side went down so the subject got negative feedback. The other three models shown here (II, I, and III-A) all make the same prediction as the subject: left-down. The numbers at the bottom of the four model columns show the number of mismatches between Pam's predictions and the model's.

Table 6 about here

Pam's s responses to the pre-test make her a perfect Model II subject. Her responses during the training sequence provide a poor fit to models I, II, and IV. Recall that the criterion for fitting Model III was that the responses be essentially random for conflict problems. Thus, although the "muddle through" prediction of Model III does not make an exact prediction on any trial, it predicts the absence of a consistent pattern over the set of conflict problems. And indeed, this is what we find in Table 6: on five of the eleven conflict problems Pam responds as if she

were relying on the weight cue, and on the other six, she conforms to the distance cue. Thus, we could simply classify Pam as a Model III subject and leave it at that.

Such an interpretation has several deficiencies. First, the classification scheme itself is unsatisfactory when compared to the others. Model III subjects get so classified as a residual category -- by the absence of any pattern in their responses to conflict problems, whereas all other classification is based on the occurrence of things that were predicted to happen, rather than the absence of things that should not. In addition to this "taxonomic" weakness, Model III's "muddle through" prediction tells us nothing about the psychological processes that actually operate when subjects detect conflict but do not yet know how to deal with it correctly. We have already cited some of the idiosyncratic strategies that different subjects bring to bear on this situation. Finally, it is important to emphasize that Table 6 represents responses during a training sequence, a situation in which the child was presumably attempting to integrate the feedback from the balance-scale's actually behavior with her current hypothesis about how it worked. None of the four models described thusfar have any mechanism to represent and utilize such information. Thus, the model to be described represents first steps in remedying these deficiencies.

Pam was run under the same conditions as Anna, and an analysis of her trial by trial explanations provided the initial evidence for the model that we eventually formulated. The most striking feature of her comments was the way she appeared to represent distance and weight on conflict problems. Both of them were treated as dichotomous: more than two weights was treated as "big", otherwise weight was "little", and if the third or fourth peg were occupied, then distance was "big", otherwise it was "little". Rather than present another lengthy protocol analysis here, we will show just two examples of this dichotomous encoding of distance.

On problem 12 (0013/1020), the child predicts left down; upon seeing the result, she says:

> Oh, now I think I know why.... I think I know because,... it's supposed to be a rule that they usually go down more if they're on that side (pointing to the extreme right of the balance scale). So that one went down cause it's 2 there (pointing far right) and none there (pointing far left).

If we encode each arm of the balance scale into a near segment (pegs 1 and 2) and a far segment (pegs 3 and 4), then this protocol is easily interpreted. "They usually go down more if they're on that side" means that if the far segment is occupied ("big distance") then the scale will tip in that direction. "Two there and none there" means that the far segment on the right is occupied by two weights, whereas the far segment on the left is unoccupied.

The second example comes from problem 14 (0200/1300), just before the child gets feedback. She says:

> This side's gonna go down (pointing left)... Even though this one has 4

> (pointing right) and this one only has 2 (pointing left)... Even though this one has (pointing right) twice as much as this (pointing left), that means that because this one's more [waves to far left] over, and that's (pointing right) all on that side.

In this case, we garner support for the dichotomous distance encoding from the comment that the weights on the right arm of the scale are "all on that side". "That side" of what? By our interpetation, they are on "that side" of the mid-point of the right arm, thus making distance "little", rather than "big" on the right.

In order to determine whether this interpretation of the protocols is valid, we need to construct a model that is consistent with Pam's actual predictions on each trial, as well as her explanations. Based upon many such comments and our interpretations of them, we constructed the model whose predictions are shown in Table 6. In order to provide a clear overview of the model we will describe it first in terms of a binary decision tree, plus a few ad hoc mechanisms. Then we will present a running production system for a more complete model based on the same underlying logic.

Figure 3 shows the binary decision tree representation for Model III-A; Pam's performance on the training sequence is shown in Table 6. The numbers under the terminal nodes correspond to the problems from Table 6 that are sorted to those nodes. The first three tests are the same as those in Model III (Figure 1), and they account for balance, weight and distance problems. If neither weight nor distance is "same", then the model begins to test for "big" values. If either weight or distance - but not both - is big, then the side with the big value determines the prediction. If both are big, then Model III-A favors whichever one is currently its criterion value. The criterion value starts as weight, but whenever negative feedback is received the criterion switches from one value to the other. The state of the criterion value is indicated in the last column in Table 6. Note that it changes after any negative feedback, not just on conflict trials with negative feedback. (The terminal node labeled "?" in Figure 3 is never reached by the set of problems in Table 6. Such a problem would be a conflict problem with neither weight nor distance "big". We have no evidence upon which to base a prediction about what the subject would do with such a problem.)

Figure 3 about here

A production system for Pam (Model III-A)

The production system for Pam is shown in Figure 4. The representation contains the actual computer listing With a few inessential details not shown) for the production system, which is written in a special language called PSG (Newell & McDermott, 1974). Appendix B contains a trace of this model running on a sequence of four problems from Table 6; one of them - Problem 5 - is also shown in Figure 5. Before we embark on a detailed description of the model, we will make a few

comments about the properties of this rather detailed representation for knowledge about the balance scale task.

Figure 4 about here

The model enables us to represent explicitly all task relevant knowledge in a homogeneous and integrated manner. This model utilizes, in one way or another, representations of knowledge about:

which side has more weight or distance,
which side has a big weight or distance,
what the current criterion value is,
what the scale was expected to do,
what the scale actually did,
whether the prediction was correct or incorrect.

The model contains rules for when and how to encode the environment. It also indicates the number and nature of pieces of information to which the subject must be responsive during the course of the experiment.

Production system interpretation

Some general properties of production systems were described earlier. In this section we will add a few more details about how the model in Figure 4 operates. Recall that the basic cycle for a production system is recognize-act. During a recognition cycle, all the productions compare their condition elements with an ordered list of elements in STM (short term memory). The trace in Figure 5 shows the state of STM after each cycle. For example at the beginning of the second cycle in Figure 5, we see that STM has 4 elements in it: (DST MORE RIGHT), (WGT MORE LEFT), (PRED), and (CRITERION WGT). An examination of the productions in Figure 4 reveals that the P1 is only production whose condition elements are completely matched by STM elements, so in this case, it fires (i.e., it is "TRUE" in Fig. 5). We can interpret a production, P:(A B C --> D E), as "If you know A and B and C (i.e. if they are currently in STM), then do actions D and E.

There are two conflict resolution principles. The first one to be applied - special case order - has already been described. If, after applying special case order, there are still two or more productions in the conflict set,then a second resolution principle - STM order - is applied. This principle chooses the productions with the frontmost element in STM. New information always enters the "front" of STM, pushing all else down a "notch". Furthermore, when a production fires, its evoking elements are moved to the front of STM (automatic rehearsal). Thus the STM order conflict resolution principle says, in effect, "when in doubt, respond to the most recently important information." (In Figure 5, and Appendix B,special case order is usually adequate to resolve conflicts. All instances where STM order is also used are explicitly indicated in the trace).

There are several different types of actions. a) STM additions. These simply add new elements to the front of STM. For example, if E3 fired, (result wrong) would be added to the front of STM. Other sources of new information are the encoding operators (described below).

b) STM modifications. Elements in STM can be altered directly. The action (A ===> B) changes symbol A to symbol B in the second element in STM. The action (X **) changes the first element in STM from a to (X (a)), [e.g. from (DOG) to (OLD (DOG))].

c) Output. These actions are surrogates for action on the external environment. The only one's used here are say.b (say "balance") and say.d (say left or right down).

Description of model (Fig. 4)

There are three major functional groups of productions.

1) Pn. These correspond to the major nodes in the decision tree representation. P1 - P4 are essentially the same as P1 -P4 in Figure 2. P5,P6,P7 correspond to the tests for Big things in Figure 3. Some of the productions use variables that can be matched by specific values in STM elements. For example, D1 and D2 can be matched by either WGT or DST, while X1 and X2 can be matched by anything.

2)En. These control the model's viewing of the balance scale after it tips, and compare what it expected to see with what it actually sees.

3)SWn. These change the criterion whenever the system determines (via the E productions) that it has made an incorrect prediction.

There are three encoding operators. None are modeled, but their conditions of evocation are explicit, as is the form of the encoding they produce.

1)Attend. Does initial encoding of weight and distance. This operator can detect sameness or difference of weight or distance and can indicate the side on which weight or distance is greater. Thus, it is only an encoding of relative quantity. The Model assumes that in the first instance this is all that is encoded.

2) Find.Big. Encodes big wgt or dst and side on which they occur (if they occur).

3) LOok. Encodes direction of tipping of scale.

Dynamics of the model.

The general procedure is as follows. First weight and distance differences, if any, are encoded. If there is no conflict, then a prediction is made, an expectation is formed, and the scale's actual behavior is observed. If it is inconsistent with the prediction, then the criterion is changed. If initial encoding reveals no clear prediction, then a second encoding is effected, this time in terms of big distance or weight. Then the rest of the process follows exactly as in the case of a single encoding.

Figure 5 contains a trace of the model working on one of the problems from Appendix B. The trace shows the state of STM at the start of each cycle, as well as which production fired. Conflicts are shown when they occur, as are the results of the encoding operators.

The system starts with an element in STM (PRED) indicating that it has a goal of making a prediction, and another element representing the current value of the criterion. Since there is no element representing weight or distance, the only production whose conditions are completely satisfied is P8, which tests for (PRED) and the absence (ABS) of a weight or distance element (D1). ATTEND, P8's only action, is an encoding operator that is modelled only up to the point of its input/output specifications. In this case the input is presumed to be the physical arrangement of disks on pegs in the configuration (0003/0020), and the outputs, as shown in the trace, are two comparative symbols indicating more weight on the left and more distance on the right. They are directly provided by the model builder.

Thus, at the beginning of Cycle 2, STM contains four elements, and these elements satisfy both P4 and P2 (see Fig. 4). P4 is a special case of P2, so it fires. It recognizes that neither weight nor distance are equal, so it attempts a second encoding (FIND.BIG) to determine some absolute amounts of distance and/or weight. Once again, an unmodelled encoding operator is assumed to produce two elements, indicating a big distance on the right and a big weight on the left. The results are shown at the start of the third cycle.

Five productions are satisfied by the elements now in STM. P2 and P4 are still satisfied since none of the elements that satisfied them on the previous cycle have been changed. P5, P6, and P7 are satisfied because they test for either big weight or big distance. Since P4 is a special case of P2 and P5 of P6 andP7 the special case order principle leaves P4 and P5 in the conflict set. But the elements that match P5 are newer than those that match P4, so STM order selects P5 to fire.

P5 matches whatever the current value of the criterion is (in this case weight) with the corresponding "big" element [in this case (WGT BIG LEFT)] and then uses the value of the directional variable (LEFT) to form its expectation (EXCEPT LEFT DOWN) and to "say" its prediction.

What the system knows at this particular moment is revealed by the contents of STM at the start of the fourth cycle. It knows that:

It expects the left side to go down	(EXPECT LEFT DOWN)
It already made a prediction	(MADE (PRED))
The current criterion is weight	(CRITERION WGT)

And it knows the encodings (WGT BIG LEFT)
(DST BIG RIGHT)
(WGT MORE LEFT)
(DST MORE RIGHT)

The rest of the trace is straightforward. During pass 4, the system seeks an encoding of what the scale actually did, and it sees that the right side went down. On pass 5 it recognizes that what it saw is discrepant with what it expected (ES), so it knows that it got the problem wrong. Finally, on the 6th pass, it recognizes that it was wrong while using the weight criterion, so it changes it to distance.

Evaluation of Representation's for Pam's Knowledge

The decision tree in Figure 3 and the production system in Figure 4 are logically equivalent: both account for all but the last of Pam's predictions during the training series. As described above, they differ from the representations of Figure 1 and 2 in that they model the subject's response to feedback, and because they both represent idiosyncratic encodings of the stimulus. Thus both models have certain advantages over the previous ones.

However, the models are not equivalent in all respects, and the psychological properties of the production system - properties previously just alluded to - can now be clarified. The production system, since it embodies a general model of the human information processing system, forces us to be very explicit about things that the decision tree lets us finesse. There is no separation of control information from data in a production system. Every relevant piece of information is explicitly represented in STM, and all task-specific knowledge for acting on that information is represented by productions. As indicated by the final list of elements in STM, we are postulating a remarkable amount of material floating around in STM. However, once we attempt to model the momentary states of knowledge for this sort of task, it becomes logically unavoidable to consider at least as much as this. It is not clear that a system that did not know all of these things could ever to the task. Such requirements are hidden in the decision tree representation. Thus it is difficult, in evaluating a decision tree representation, to be sure just how plausible the model is with respect to the psychological demands it might impose on the organism.

For all their emphasis on the importance of the outputs from the encoding operators however, the production system models do not describe the encoding process itself. Neither do they indicate precisely what sort of encoding deficit might affect response to instruction. A remedy to the former limitations would take the form of a model of encoding, and we leave that for future investigation. The second issue, that of the nature and effect of encoding deficits, is directly related to Q4 and Q5 of our initial set. In the third experiment in this series, we investigated these issues.

Experiment 3: The Encoding Hypothesis

Recall that the results of Experiment 2 indicated that older and younger children, equated for initial task specific knowledge about the balance scale, responded quite differently to the training sequences. This finding motivated a shift in the representation and in the level - or grain - of our analysis of what was going on during training. Anna's protocol analysis revealed her difficulty in determining the appropriate encoding of the two relevant dimensions, and the analysis of Pam's responses during training led to a production system which incorporated two levels of encoding - one relative, one absolute (big/not big) - for both dimensions. Similarly fine-grained analysis of other protocols revealed many such stimulus misencodings. This suggested to us that differential encoding might be the cause of the differential responsiveness to instruction.

However, in order to convincingly test this hypothesis, several steps are necessary. First we must assess encoding independently of predictive performance. Then we must show that the appropriate manipulation can eliminate or at least reduce encoding differences. Finally we must demonstrate that when the difference on the explanatory variable - encoding - is eliminated, the initially observed difference on the to-be-explained variable - responsiveness to instruction - is also eliminated. In summary then, our goal is to show that in a group of older and younger children who are all using Model I initially, there is a consistent encoding deficit in the younger children, then to eliminate this deficit, and finally to expose both groups to the training sequence and to produce identical learning in both age groups.

Attempting to do this at the fine-grained level of the preceding section would lead to a mass of detailed variation that would be likely to obscure the general properties of encoding differences; it would also be prohibitively expensive in terms of time and effort. Therefore, in this section, we move back up to the aggregate level of grouped data.

The reconstruction paradigm.

Chase and Simon (1973) utilized a reconstruction paradigm in order to study the differential ability of chess masters and non-masters to extract meaningful information from briefly presented board configurations. This procedure suggested to us a means by which differences between older and younger children's encoding of balance scale configurations could be assessed independent of their predictions about the effect of these configurations on the scale's behavior.

In the third experiment in this series, five- and eight-year-old children were presented with various configurations of weights on a balance scale for a few seconds (the scale was not free to tip). Then the scale was removed from view, and they were required to reconstruct as accurately as possible the initial configuration on an empty scale. Note that this procedure allowed independent assessment of encoding on both weight and distance dimensions. For example, when given an initial configuration (0300/0200) the child might reconstruct it as (03C0/0200), or

(0030/2000), or (0200/0100) or (0010/0003), revealing , respectively, no misencoding, distance only misencoding, weight only misencoding, or both weight and distance misencodings. Our protocol analyses led us to expect that the older children would be accurate on both dimensions, while the younger children would do well on weight, but poorly on distance.

Basic procedure. The same basic procedure was followed in all phases of Experiment 3, and the full details are given in Siegler (1976b). Here we will only describe the major features. Overall, 40 kindergartners ("five-year-olds") and 30 third-graders ("eight-year-olds") from two public schools in Pittsburgh participated in Experiment 3.

Two identical balance scales were used. They were slightly different from the one used previously, having 7, rather than 4, pegs on each side of the fulcrum, and having a built-in lever, rather than wood blocks, to keep the scale from tipping until the experimenter released it. A large styrofoam board was used to hide one of the balance scales during the reconstruction phases.

The encoding test included 16 problems, on each of which there were from 3 to 5 weights on each side, all located on either the third, fourth or fifth peg from the fulcrum. On any given problem, only one peg on each side was occupied.

Children were tested individually in a vacant room in their school. Each child was presented with the encoding test first, and then presented with the same 24 item predictions task (without feedback) used in the Experiment 2 posttest. For the encoding test, the children were told:

> The idea of the first game is for you to look how the weights are set on the pegs on my balance scale and then make the same problem by putting the weights on the pegs on yours. First I'll put the weights on the pegs on my scale. You should watch closely to see how the weights are set on the pegs. Then I'll put the styrofoam board back up so you can't see my scale. You will then need to put the weights on the pegs on your scale in the same way that you saw them on my scale. Just put the weights on the pegs so it's just like the problem you saw on my scale.

After the first trial, children were again told, "Remember, you should watch closely to see how the weights are on the pegs on my scale so that you can put the weights on your scale in the same way." Children were allowed 10 seconds to observe the initial configurations, and then they were allowed to reconstruct the arrangement immediately on the other scale. There was no time limit for reconstruction, although children usually finished quickly.

Following the last encoding trial, children were told that they were to play another game, and instructions similar to the previous predictions trials were given. The encoding and predictions tasks were given in a single session lasting about 25 minutes.

There were several variations on this basic procedure. We will describe each variation and its results in sequence. The results from all phases are shown in three forms. Table 7 shows the percentage of correct distance and weight encodings for both age groups. A strict criterion of perfect reconstruction of both sides of the scale was used for both weight and distance scoring. Table 8 shows the percentage of correct predictions for each type of problem, and Table 9 shows the classification by model type for each age group in each phase of Experiment 3.

Experiment 3a. Ten children from each age level participated in the experiment exactly as described above. As shown in Table 7, the results were consistent with the encoding hypothesis. The younger children showed a great disparity between their ability to reproduce weight perfectly and their ability to reproduce distance , while the older children did not show a significant difference between their weight and distance reproductions. This pattern held for individual subjects in each age group, and is not the result of aggregating over subjects (see Siegler, 1976b, for extensive statistical analyses of these results). Notice that these encoding differences between older and younger children were not accompanied by a corresponding difference in ability to predict how the balance scale would behave. As shown in Tables 8 and 9, there was virtually no difference in the percentage of different types of problems passed or in the distribution of children using each model.

Experiment 3b. In this variant, 10 five-year-olds were given 15 rather than 10 seconds to view the initial configuration during the encoding tests. This was done to explore the possibility that the younger children were simply a bit slower than the older ones in encoding the configurations. If they were attempting to encode both dimensions, and had a preferred noticing order of weight first, then giving them more time would be expected to improve their distance scores. As shown in Table 7, this "insufficient time" explanation is unsupported by the results.

Experiment 3c. Perhaps the younger children did not understand what was meant by "make the same problem". In this variant, the children were told explicitly what to encode, and what constituted the experimenter's criterion for the "same" problem. Ten children of each age level participated. The instructions for the encoding task were changed to the following

> The idea of the first game is for you to look how the weights are set on the pegs on my balance scale and then to make the same problem by putting the weights on the pegs on yours. You want it to be the same problem in two ways. You want the same number of weights on each side of your scale as I had on my scale, and you want the weights on each side of your scale to be the same distance from the center as they were on my scale....

Later in the instructions, children were again told that they should "watch closely to see how the weights are set on pegs - how many there are on each side and how far from the center the weights on each side are." Finally, at the end of the instructions, children were asked to indicate the two ways their arrangements should be like the experimenter's. This was to ensure that they understood what they had been told. The few children who did not understand were again presented the

instructions and asked the identical question until they could answer appropriately. In all other ways, the procedure was the same as that used in Experiment 3b, with a 15 second viewing period.

Once again, as shown in Tables 7, 8, and 9, the results differed hardly at all from those of 3a and 3b. Telling children what to encode does not reduce the discrepancy between their encoding of weight and distance, nor does it improve their performance on the predictions task.

Tables 7, 8, and 9 about here

Experiment 3d. This time, children were told not only what to encode, but also how to encode it. If the problem lay in the inability of the younger children to correctly encode distance, or to handle two dimensions simultaneously, then perhaps direct instruction might help them. Ten children of each age group were given the following additional instructions during the encoding trials:

> You do it like this. First you count the number of weights on this side - one, two, three, four. Then you count the number of pegs the weights are from the center - first, second, third. So you say to yourself 'four weights on the third peg.' Then you would do the same for the other side - one, two, three, four, five weights on the first, second, third peg. So it would be five weights on the third peg. Then you would say 'four weights on the third peg and five weights on third peg.' Then you would put the right number of weights on the right pegs on each side. Let's practice one.

This was followed by seven practice trials on which the child received feedback on the correct counting of weights and distances. This procedure was expected to reduce or eliminate the weight-distance discrepancy for the younger children, but since the older children presumably already knew how and what to encode, it was not expected to affect their performance. No effect was expected on the predictions performance of either group. All of these expectations were confirmed. Table 7 shows that the younger children performed equally well on weight and distance, and that the older children performed, as before, better overall, but with no weight-distance discrepancy. Tables 8 and 9 show that the predictions performance of both groups was indistinguishable from previous results.

Experiment 3e. Having finally eliminated the encoding deficit between weight and distance for the younger children, the question remains as to whether that deficit really was the cause of the differential responsiveness to instruction that we initially set out to explain. In this final experiment, the same children who participated in Experiment 3d were given the conflict training sequence used in Experiment 2 a few days after they completed 3d. According to the encoding hypothesis, both older and younger children should now benefit from experience with conflict problems that previously had benefitted only the older children. Following the training sequence, the predictions test (without feedback) was again

given to the two groups. The results of this post-training predictions test are shown in row 3e of Tables 8 and 9. Note that rows 3d and 3e are based on the same set of subjects at different times. The sequence of manipulations and their corresponding results were: i) Instructions about what and how to encode, ii) encoding task [Table 7, 3d], iii) predictions task [Tables 8 and 9, 3d], iv) conflict training with feedback, a few days later, v) repeat of predictions task [Tables 8 and 9, 3e].

Comparison of rows d and e in Tables 8 and 9 shows that training now aided both age groups. Although there appears to be a slight advantage overall for the older children, there were no significant effects for either age alone, or an age-problem type interaction. It seems clear then, that the qualitative differences in responsiveness to training were eliminated by prior training in encoding. Although the younger children did not benefit as much as the older, it should be remembered that their encoding performance also did not reach the level of the older children.

Representing the encoding process

Let us return to the issue of the appropriate representation for knowledge about the balance scale. The results of Experiment 3 provide strong support for the encoding hypothesis: younger children clearly do not tend to encode the distance dimension in this task. Without such encoding, they can derive little benefit from the instruction series. However, if given careful and explicit instruction on encoding, they do begin to do it correctly, and such improvement subsequently enables them to benefit spontaneously from a training sequence. How can we represent this phenomenon?

One desirable property of a good representation for this situation would be an explicit model of the encoding process. This would require replacing the unmodelled encoding operators of the kind used in the production system for Pam (Fig 4) with explicit productions that scanned the stimulus and returned some encoded representation. Another requirement would be a general self-modification capacity with two distinguishable capabilities. One capability would deal with the construction of procedures that directly followed instructions, as did the children who were told how to encode by counting. Another capability would represent the rule-induction or concept formation procedure that underlies learning from the training series. Pam's production system is at least minimally sensitive to feedback about the correctness of the current hypothesis; much more remains to be done.

The construction of such a model would necessitate further specific assumptions about the precise nature of the information processing that goes on in this situation, and such assumptions would have to be independently tested in other experimental paradigms. Such extension might include reaction time studies that compared conventional representations with their symbolic equivalents (to bypass the encoding stage), reconstruction memory for just- predicted problems, and more general rule induction tasks.

Types of Knowledge in the Human Information Processing System

Our exploration of the issues surrounding the evaluation of different representations for knowledge has revealed that it is possible to distinguish between several different types of knowledge. The suitability of a representation depends upon the particular type of knowledge in which we are interested. In this final section, we will briefly indicate what appear to us to be distinctly different kinds of knowledge. The order in which they are described corresponds roughly to their degree of permanence and stability in the human information processing system.

K1: knowledge about the momentary state of affairs. This is the knowledge represented by the elements in STM in a production system, or in the more general concept of "active memory" in other cognitive theories. In a production system, all the productions are continually attempting to recognize familiar elements of K1, and to act upon it through modification. K1 represents what is "going on" from one moment to the next. It contains information about the environment that has been produced by encoding operations, and by the actions of satisfied productions. It constitutes a record of the system's immediate past.

K2: Knowledge about how to do a task or solve a problem. This type of knowledge is represented by decision trees of the sort used in Figs 1 and 3, or by the productions in a production system. The knowledge in K2 typically consists of tests for the type of knowledge represented by K1. A production system provides a convenient and flexible representation for K1 and K2. However, many of the explicit assumptions in such representations have no particular psychological relevance, while others, although important, may not be amenable to independent experimental verification. Thus the evaluation of production system representations for K2 rests upon multiple level converging empirical measures, including global responses, protocols, and reaction times. Although many particular assumptions may be unverifiable, the integrated behavior of the total system can be observed and evaluated.

K3: knowledge about how to describe K2. A frequently discussed issue in developmental psychology concerns the relative validity of explanations versus performance(cf. controversy between Braine, 1964, and Smedslund, 1965). In our experiments we found that the two forms of measurement were highly correlated, although they did reveal some interesting differences in the Model III children. It would seem that all explanations tasks require that the child have a type of knowledge that is distinct from performance knowledge as such, although it is rarely modelled or represented explicitly in psychological theories.

K4: knowledge about how to modify K2 and K3. This is the knowledge required for both learning in the long term, and immediate self-modification according to task demands. Some of the general properties of representations for this sort of knowledge have been discussed by Klahr (1976a,b) and Newell (1972a). The content of K4 would be a theory of learning, and it would be premature to even imply that such a full blown theory is near at hand. However, recent and on-going work with self-modifying production systems suggests that this is a very promising form of representation for K4 (Newell, 1976; Waterman, 1974).

K5: knowledge about how to interpret the knowledge stated at the other levels. This knowledge would include, in the case of a production system representation, all the rules that the interpreter has to have in order to run a production system. It is the base level knowledge in the system, presumed to be functionally equivalent to the basic system architecture. It is probably inaccessible to introspection, or to instruction, although it may undergo development.

Conclusion

Representation of children's knowledge requires that we make testable assertions about both the basic encoding of the environment and the processes that operate on those encodings. Cognitive development and instructional procedures involve changes in both the encoding operators and the rule systems. Instruction will tend to be ineffective if the instructional situation is encoded by the learner in a manner that is unexpected by the instructor. In a limited domain, we have demonstrated that such misencoding was indeed occurring, that we could locate the point of difficulty, eliminate it and have instruction proceed as we expected it to.

From a broader viewpoint, we have tried to show that the appropriate representation for knowledge depends upon the goals of the scientific endeavor. Different kinds of knowledge are best represented by different formalisms, and are best investigated by different empirical procedures. This pluralistic view of knowledge representation may facilitate our understanding of, and influence upon, what it is that children know.

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Table 1

Predictions for percentage of correct answers and error patterns on posttest for children using different models

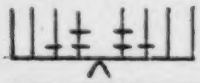
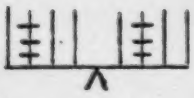
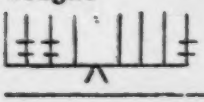
Problem Type	Models				Predicted Developmental Trend
	I	II	III	IV	
Balance 	100	100	100	100	No change--all children at high levels
Weight	100	100	100	100	No change--all children at high level
Distance 	0 (Should say "balance")	100	100	100	Dramatic improvement with age
Conflict-weight 	100	100	33 (Chance responding)	100	Decline with age Possible upturn in oldest group
Conflict-distance	0 (Should say "right down")	0 (Should say "right down")	33 (Chance responding)	100	Improvement with age
Conflict-balance	0 (Should say "right down")	0 (Should say "right down")	33 (Chance responding)	100	Improvement with age

Table 2

Developmental trends observed and predicted on different problem-types in Experiment I (percentage of problems predicted correctly)

Number of each type	Problem Type	Age				Predicted Developmental Trend (From Table I)
	Grade	K-1st	4th-5th	8th-9th	11th-12th	
	Age (years)	5-6	9-10	13-14	16-17	
	Mean age (mos)	73	120	169	207	
4	Balance	94	99	99	100	No change--All children at high level
4	Weight	88	98	98	98	No change--All children at high level
4	Distance	9	78	81	95	Dramatic improvement with age
6	Conflict-weight	86	74	53	51	Decline with age--Possible upturn for olde
6	Conflict-distance	11	32	48	50	Improvement with age
6	Conflict-balance	7	17	26	40	Improvement with age
	Weighted mean %	46	61	62	67	

Table 3

Number of children fitting each model

Age	I	II	III	IV	Unclassifiable
5-6	23	0	0	0	7
9-10	3	9	12	2	4
13-14	3	7	17	1	2
16-17	0	6	19	5	0
Total	29	22	48	8	13

Table 4

Number of children in Experiment 1 fitting each model--predictions and explanations criteria

		Rule by Predictions Criterion			
		I	II	III	IV
Rule by Explanations Criterion	I	23	1	0	0
	II	0	7	1	0
	III	0	13	46	0
	IV	0	0	0	8

Table 5

Number of children using different models--Experiment 2

		Model I	Model II	Model III	Unclassifiable
	Control	8	0	0	2
5-year-olds	Distance training	3	4	1	2
	Conflict training	5	0	0	5
	5's Total	16	4	1	9
	Control	5	3	0	2
8-year-olds	Distance training	0	8	1	1
	Conflict training	0	2	5	3
	8's Total	5	13	6	6
	Grand Total	21	17	7	15

Table 6

Pam on training sequence, and predictions from 4 models

Problem					Prediction				
Number	Configuration	Type	S2	feedback	IV	II	I	III-A	Criterion
1	0200/0200	D	L		L	L	B	L	W
2	0020/0200	B	B		B	B	B	B	
3	0020/3000	CD	R	--	L	R	R	R	
4	0003/0100	CW	L		L	L	L	L	d
5	0200/0400	CW	L	--	R	R	R	L	
6	0102/2010	B	B		B	B	B	B	W
7	0003/0020	CD	L	--	R	L	L	L	
8	0100/0200	CW	L	--	R	R	R	L	d
9	0040/1020	CW	L		L	L	L	L	W
11*	0001/2000	W	R		R	R	R	R	
12	0013/1020	CD	L	--	R	L	L	L	
13	0120/2200	CD	L		L	R	R	L	d
14	0200/1300	CW	L	--	R	R	R	L	
15	0002/0010	CD	R		R	L	L	R	W
16	0023/1110	CW	R	--	L	L	L	L	
					7	6	7	1	
Pretest									
1	100/100	D	L			L			
2	010/300	CW	R			R			
3	100/200	CD	R			R			
4	010/020	W	R			R			
5	020/002	D	R			R			
6	200/400	CD	R			R			
7	100/200	CD	R			R			
8	030/020	W	L			L			

*Note: Problem 10 was omitted

Table 7

Percentage of correct encodings--Experiment 3

	5-year-olds		8-year-olds	
Experiment	Weight Encodings	Distance Encodings	Weight Encodings	Distance Encodings
3a	51	16	73	56
3b	54	9		
3c	54	19	64	73
3d	52	51	72	76

Table 8

Percentage of correct predictions--Experiment 3

Experiment	Age	2 Balance	2 Weight	2 Distance	6 Conflict-Weight	6 Conflict-Distance	6 Conflict-Balance
3a	5-year-olds	95	100	8	100	2	0
	8-year-olds	98	100	5	100	0	0
3b	5-year-olds	85	85	18	92	8	2
3c	5-year-olds	72	90	18	72	12	15
	8-year-olds	100	98	30	90	20	0
3d	5-year-olds	72	92	22	86	17	6
	8-year-olds	100	100	22	100	0	0
3e	5-year-olds	92	89	72	89	33	0
	8-year-olds	100	100	94	67	50	0

Table 9

Number of children using different models--Experiment 3

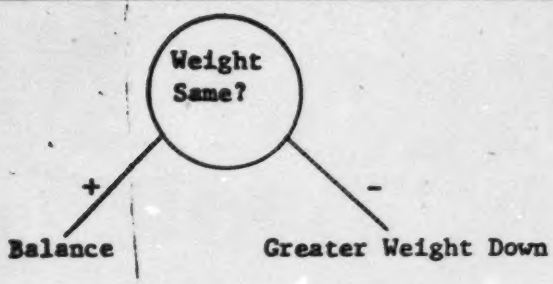
Experiment		Rules Used I	II	III	Unclassifiable
3a	5-years	9	0	0	1
	8-years	8	1	0	1
3b	5-years	7	0	0	3
3c	5-years	7	0	0	3
	8-years	6	2	1	1
3d	5-years	6	0	0	4
	8-years	6	1	0	3
3e	5-years	1	3	4	2
	8-years	0	3	7	0

Figure Captions

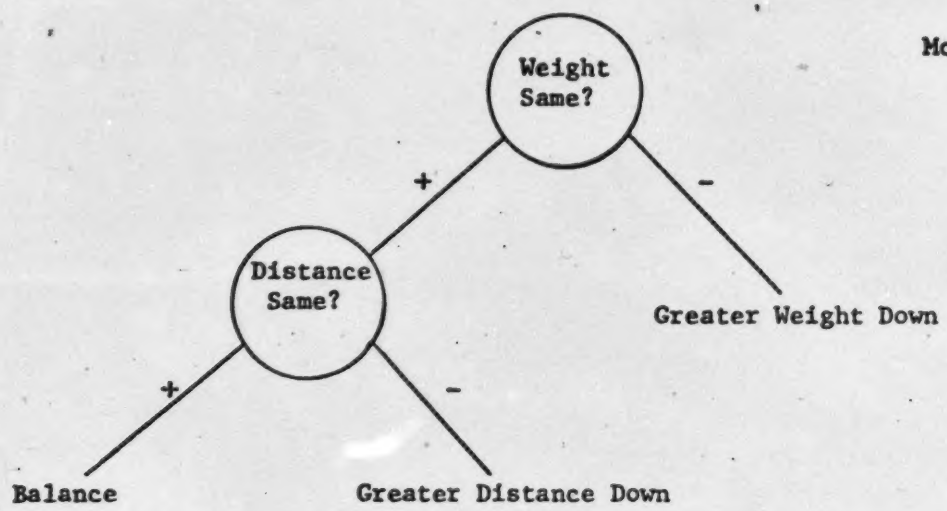
Figs and Tables	
Figure 1	Decision tree representations for four models of balance scale predictions
Figure 2	Production system representations for four models
Figure 3	Decision tree representation for Pam's prediction model
Figure 4	Production system for Pam
Figure 5	Trace of Pam's production system running on a conflict-distance problem

Figure 1

Model I



Model II



Models III and IV

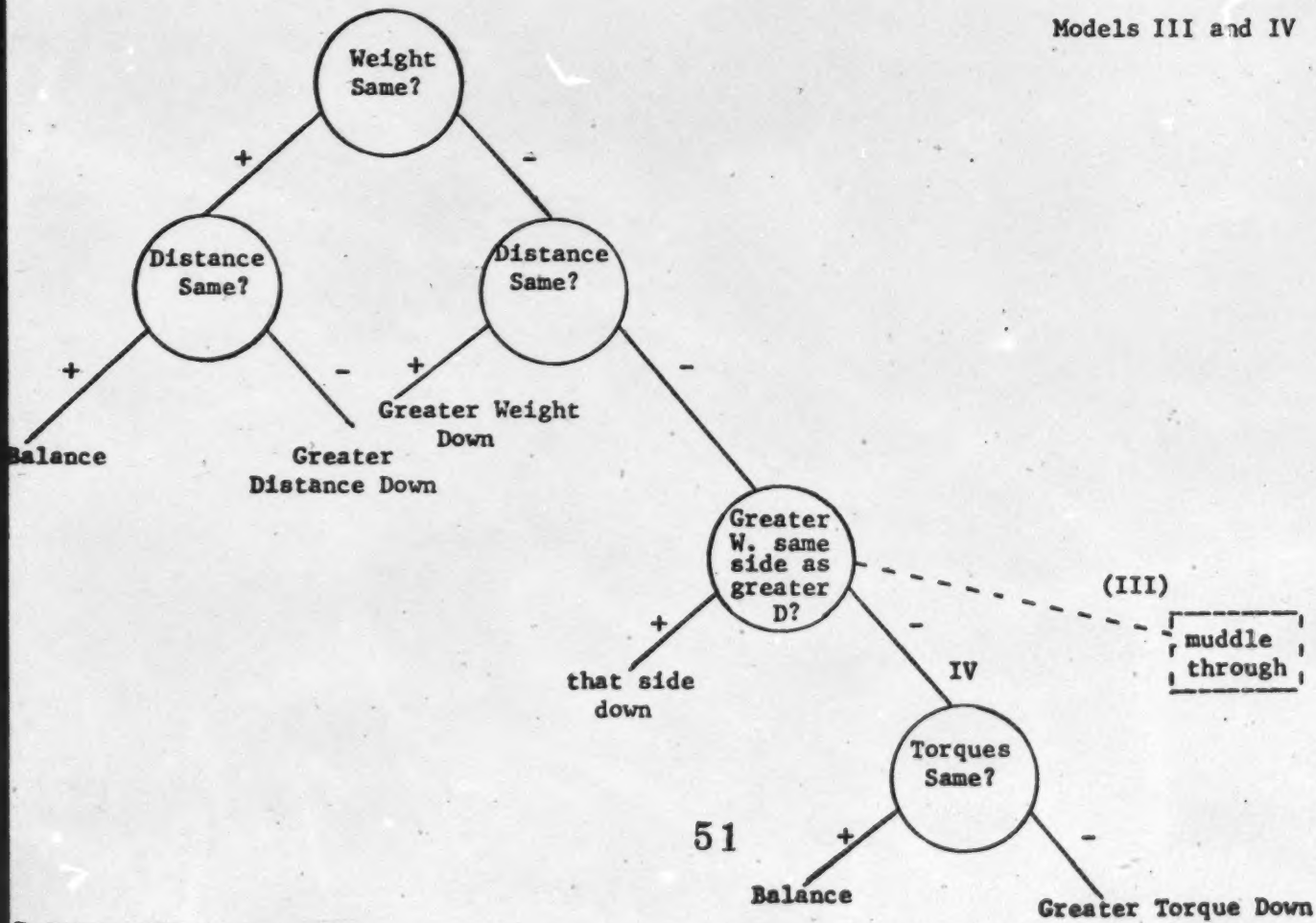


Fig 2

Model I

P2:((Side X more W) --> (Say X "down"))
P1:((Same W) --> (Say "balance"))

Model II

P3:((Same W) (Side X more D) --> (Say X "down"))
P2:((Side X more W) --> (Say X "down"))
P1:((Same W) --> (Say "balance"))

Model III

P5:((Side X more W) (Side X more D) --> (Say X "down"))
P4:((Side X more W) (Side X less D) --> muddle through)
P3:((Same W) (Side X more D) --> (Say X "down"))
P2:((Side X more W) --> (Say X "down"))
P1:((Same W) --> (Say "balance"))

Model IV

P7:((Side X more Torque) --> (say X "down"))
P6:((Same Torque) --> (Say "balance"))
P5:((Side X more W) (Side X more D) --> (Say X "down"))
P4':((Side X more W) (Side X less D) --> (get Torques))
P3:((Same W) (Side X more D) --> (Say X "down"))
P2:((Side X more W) --> (Say X "down"))
P1:((Same W) --> (Say "balance"))

	Transitional requirements	
	Productions	Operators
I -> II	add P3	add distance encoding and comparison
II -> III	add P4, P5	
III -> IV	modify P4, add P6, P7	add torque computation and comparison

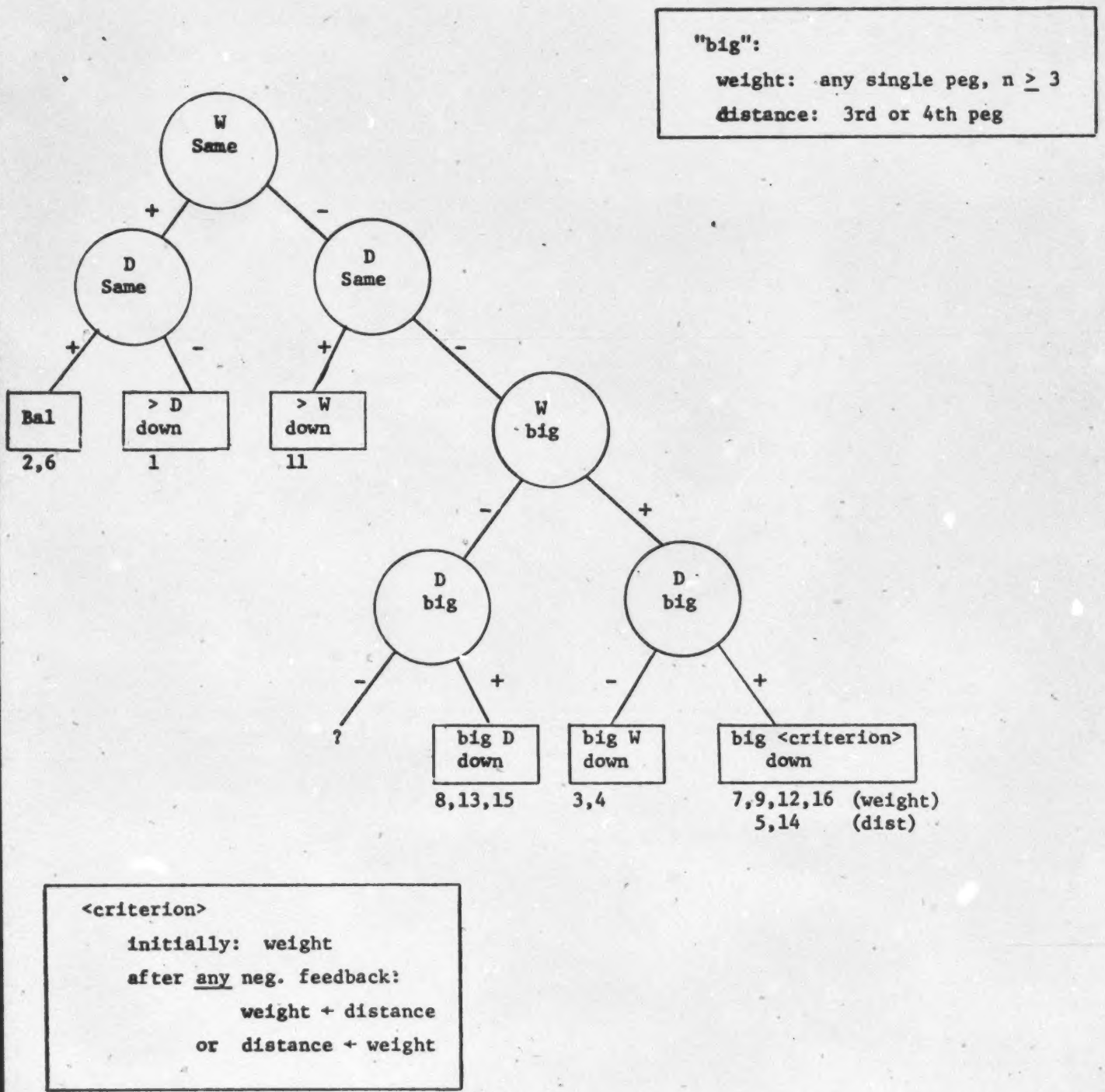


Figure 3

Model III - a

(Pam)

Figure 4. PS for III-A

```
D1:(CLASS wgt dst) D2:(CLASS wgt dst)

P1:((pred) (wgt same) --> (made **) (expect balance even) say.b)
P2:((pred) (wgt more X1) --> (made **) (expect X1 down) say.d)
P3:((pred) (wgt same) (dst more X1) --> (made **) (expect X1 down) say.d)
P4:((pred) (wgt more)(dst more) --> find.big)
p5:((pred) (criterion D1)(D1 big X1)(D2 big X2) --> (made **) (expect X1 down)say.d)
P6:((pred) (wgt big X1) --> (made **) (expect X1 down) say.d)
P7:((pred) (dst big X1) --> (made **) (expect X1 down) say.d)
P8:((pred)(D1) abs --> ATTEND)

e1:((expect) --> look)
e2:((expect x1 x2)(see x1 x2) --> (did **)(see ===> saw)(result correct))
e3:((expect x1 x2)(see x1 x2) abs (see) --> (did **)(see ===> saw)(result wrong))

sw1:((result wrong)(criterion dst) --> (old **)(dst ===> wgt))
sw2:((result wrong)(criterion wgt) --> (old **)(wgt ===> dst))
sw3:((result correct)(criterion) --> (old **))

find.big:(OPR CALL) ;returns (wgt|dst big left|right), one or two such.
look:(OPR CALL) ; looks for result of balance tipping.
                _ ; returns (see left|right down)
attend:(OPR CALL) ; initial encoding of same or difference on dst & wgt
                    ;returns (wgt|dst same|more left|right)
```

Figure 5. Trace of Pam's production system running on problem 7.
(0003/0020)

```
Cycle 1
  STM: ((PRED) (CRITERION WGT))

  TRUE: P8: ((PRED) (D1) ABS --> ATTEND)
       Output from ATTEND (input to STM) ::> (wgt more left)(dst more right)

Cycle 2
  STM: ((DST MORE RIGHT) (WGT MORE LEFT) (PRED) (CRITERION WGT) )
     CONFLICT.SET: (P2 P4)
  TRUE: P4: ((PRED) (WGT MORE) (DST MORE) --> FIND.BIG)
       Output from FIND.BIG (input to STM) ::> (dst big right)(wgt big left)

Cycle 3
  STM: ((WGT BIG LEFT) (DST BIG RIGHT) (PRED) (WGT MORE LEFT) (DST MORE RIGH
T) (CRITERION WGT))
     CONFLICT.SET: (P2 P4 P5 P6 P7)
     CONFLICT.SET: (P4 P5) AFTER SPECIAL.CASE.ORDER
     CONFLICT.SET: (P5) AFTER STM.ORDER
  TRUE: P5: ((PRED) (CRITERION D1) (D1 BIG X1) (D2 BIG X2) --> (MADE **) (EXPE
CT X1 DOWN) SAY.D)

********** LEFT down

Cycle 4
  STM: ((EXPECT LEFT DOWN) (MADE (PRED)) (CRITERION WGT) (WGT BIG LEFT) (DST
 BIG RIGHT) (WGT MORE LEFT) (DST MORE RIGHT))
  TRUE: E1: ((EXPECT) --> LOOK)
       Output from LOOK (input to STM) ::> (see right down)

Cycle 5
  STM: ((SEE RIGHT DOWN) (EXPECT LEFT DOWN) (MADE (PRED)) (CRITERION WGT) (W
GT BIG LEFT) (DST BIG RIGHT) (WGT MORE LEFT) (DST MORE RIGHT))
     CONFLICT.SET: (E1,E3)
  TRUE: E3: ((EXPECT X1 X2) (SEE X1 X2) ABS (SEE) --> (DID **) (SEE ===> SAW)
(RESULT WRONG))


Cycle 6
  STM: ((RESULT WRONG) (DID (EXPECT LEFT DOWN)) (SAW RIGHT DOWN) (MADE (PRE
D)) (CRITERION WGT) (WGT BIG LEFT) (DST BIG RIGHT) (WGT MORE LEFT) (DST MORE R
IGHT))
  TRUE: SW2: ((RESULT WRONG) (CRITERION WGT) --> (OLD **) (WGT ===> DST))

Cycle 7
  STM: ((OLD (RESULT WRONG)) (CRITERION DST) (DID (EXPECT LEFT DOWN)) (SAW
RIGHT DOWN) (MADE (PRED)) (WGT BIG LEFT) (DST BIG RIGHT) (WGT MORE LEFT) (DST
MORE RIGHT))
```

Appendix A. Protocol excerpts of 5-year old on traing sequence.

00400 T1 0001/2000 4:46
00500
00600 E. Okay. Let's put these two here, and this one here.
00700 S. This side will go down (points left).
00800 E. Which side? Touch the side that will go down.
00900 S. (touches left side)
01000 E. Okay. Let's see if you were right. [Removes blocks. Scale tips:
01100 left-up;right-down.] Were you right?
01200 S. (nods no)
01300 E. Which side went down?
01400 S. (points right)
01500 E. Okay. Why do you think that was? Why did you think before this side
01600 would go down?
01700 S. 'Cause that one (points left) didn't have as much as that one (points
01800 right).
01900 E. Uh-huh. But what actually happened?
02000 S. This side went down because that one's heavier (points right).
02100
02200 T3 0100/1000 6:10
02300
02400 E. Okay. What do you think will happen this time?
02500 S. They will both stay up.
02600 E. Why do you think that?
02700 S. 'Cause they are both the same.
02800 E. Let's see if you are right. [Removes blocks. Scale tips:Left
02900 down.] Were you right?
03000 S. (nods yes)
03100 E. You were? Look. Do they both...Are they balanced? Is it like it was
03200 before?
03300 S. Well, why are they both the same thing and one's up and one's down?
03400 E. Why do you think that is?
03500 S. I don't know.
03600
03700 T4 0020/0020 7:00
03800
03900 E. Okay. What do you think will happen this time?
04000 S. The same again.
04100 E. They will stay the same again. Why do you think that?
04200 S. 'Cause. Wait a minute. It won't.
04300 E. It won't?
04400 S. 'Cause this one (points left) is closer to this one (points to fulcrum).
04500 And this one (points right) is closer to this one (points to fulcrum).
04600 E. So what will happen?
04700 S. This side (points right) will go up.
04800 E. This side will go up?
04900 S. Uh-huh.
05000 E. Okay. What do you mean by "up"? Point which way it will go.

05100 S. I think....
05200 E. Which?
05300 S. ... it will go down.
05400 E. This side will go down (points left) ?
05500 S. Uh-huh.(Nods "yes")
05600 E. And this side ... and so it will be like this ?(tilts balance
05700 manually : left-down;right-up)
05800 S. Uh-huh.
05900 E. Is that right?
06000 S. Uh-huh.
06100 E. Okay, let's see if you are right. [Removes blocks. Scale tips:
06200 right-down] Were you right?
06300 S. (nods no)
06400 E. What happened?
06500 S. This went down (points right).
06600 E. Why do you think that is?
06700 S. I don't know!
06800 E. Well, think about it.
06900 S. Ummmm.
07000 E. Okay.
07100 S. I just don't know why.
07200 E. You just don't know why.
07300 S. Uh-huh.
07400 E. Well, we'll keep on working and maybe you'll figure it out.
07500
07600
07700
07800 T6 0102/2010 9:43
07900
08000 E. Okay, what will happen on this one?
08100 S. Yes. This side (points right) will both stay the same (points to
08200 both sides).
08300 E. Let's see if ...Why do you think that?
08400 S. Because they both look the same. One is empty in the middle and
08500 one is empty in the middle.
08600 E. Okay. (scale balances)..Were you right?
08700 S. (nods yes)
08800 E. Uh-huh. You were. That's right.
08900 S. I was right!
09000 E. That's right.
09100
09200
09300 T7 0200/2000 10:25
09400
09500 E. All-righty. Now, what will happen this time?
09600 S. This side (points left) is farther away from this, (indicates
09700 fulcrum) and this side (points right)is closer to this.
09800 (indicates fulcrum) So, I think this side (points left) will go
09900 up. And this side will go down (points right).
10000 E. Let's see if you are right.(removes blocks:left-down) Were you right?

10100 S. Huh-uh.(no)
10200 E. What happened?
10300 S. (points left, center, right and up)
10400 E. What?
10500 S. This went up (points right) and this went down (points left).
10600 I thought this would go up (points left).
10700 E. Okay. Try to figure out what's happening.
10800 S. H'm. I don't know why.
10900 E. Well you just keep on trying to figure out.
11000
11100
11200
11300 E7 0003/0004 26:46
11400
11500 S. I'm ready. Ha, wait a minute. I forgot. I did it wrong. I gotta think
11600 ...(can't hear). This is four. This is three. This one will go down
11700 (points right).
11800 E. What do you think would happen if we put one more here? What do you
11900 think would happen? [0004/0004]
12000 S. Both stay the same. This one is crooked a little bit (adjusts right
12100 weights).
12200 E. What do you think'll happen?
12300 S. Stay the same.
12400 E. Yeah? Let's see if you're right. [Removes blocks. Scale tips
12500 right-down, with sharp rap as it hits table.]Did they?
12600 S. No!
12700 E. No? No, they didn't. Did they?
12800 S. Plunk. Plunk.
12900 E. Plunk! Why do you think that was?
13000 S. I don't know. They both had four. See, one-two, (coun's left) one-two
13100 -three-four; (counts right) one-two-three-four.
13200 E. They both have four. Is that what made this side go down so much
13300 and this side go up so much?
13400 S. No.
13500 E. What do you think it was?
13600 S. I don't know.
13700 E. Think about it. What could it be?
13800 S. I just don't know.
13900 E. Just don't know. Look at it for a moment and try to figure out
14000 what it could be. Real carefully.
14100 S. This one is far away (points right) and this one is close (points
14200 left).
14300 E. Okay. Have any other ideas?
14400 S. Unh-unh (No).
14500
14600
14700 E8 0003/3000 28:40
14800
14900 E. Okay. Now, want to make up another problem?
15000 S. Uh-huh.

15100 E. Okay.
15200 S. This one is gonna be a good one. Stay the same.
15300 E. You think so?
15400 S. Uh-huh.
15500 E. Okay, let's see if you're right. [Removes blocks. Scale balances]
15600 Were you right?
15700 S. Uh-huh!
15800 E. Yeah, you were.
15900 S. I'm being right and right and right, but one time I was wrong.
16000
16100
16200
16300 E9 0003/0003 29:26
16400
16500
16600 E. [Requests information on how scale workss, and
16700 about what would happen on this trial]
16800 S. There's three, and this side (points right) would go down, I guess.
16900 E. That side would go down?
17000 S. And this side would go up (points left).
17100 E. Why?
17200 S. Because this is far away (points right) and this is close (points left).
17300 So I think it would.
17400 E. Think so?
17500 S. Uh-huh.
17600 E. Let's see if you're right.
17700 S. Ohh! Right!
17800
17900 E. What would you do to make it balance, now? [S. starts
18000 to move scale manually to balance position] No...I mean by
18100 moving the little...little circles around. What could
18200 you do to make that balance?
18300 S. This three here (points to righ', first peg), and this three stay
18400 here (points left). [0003/3000]
18500 E. Let's see if that's right, what you do.
18600 S. I have to hold this up. (lifts right side and moves weights). [0003/3000]
18700 E. Are you right?
18800 S. (nods yes)
18900
19000 E. What would you do to make the other side go down?
19100 S. Whoops. [3000/3000] That side will go up. [points right] Whoops, there.
19200 E. Why does that happen?
19300 S. Because that one's far away (points left) and that one's close (points
19400 right).
19500 E. I see.
19600
19700 S. But if I both had them far away. [3000/0003] Both sides would go
19800 down. (giggle) They balance.
19900

Appendix B

Trace of ps for Model III-A. on four problems

```
>;run on problem 5.  assume criterion set to distance
>;     (0200/0400)

0.  STM: ((PRED) (CRITERION DST))
  TRUE: P8: ((PRED) (D1) ABS --> ATTEND)
        ATTENDING - INPUT NEXT STIMULUS = >(wgt more right)(dst more

1.  STM: ((DST MORE LEFT) (WGT MORE RIGHT) (PRED) (CRITERION DST) )
      CONFLICT.SET: (P2 P4)
  TRUE: P4: ((PRED) (WGT MORE) (DST MORE) --> FIND.BIG)
        ATTENDING - INPUT NEXT STIMULUS = >(wgt big right)(dst big le

2.  STM: ((DST BIG LEFT) (WGT BIG RIGHT) (PRED) (WGT MORE RIGHT) (DST
-T) (CRITERION DST))
      CONFLICT.SET: (P2 P4 P5 P6 P7)
      CONFLICT.SET: (P4 P5) AFTER SPECIAL.CASE.ORDER
      CONFLICT.SET: (P5) AFTER STM.ORDER
  TRUE: P5: ((PRED) (CRITERION D1) (D1 BIG X1) (D2 BIG X2) --> (MADE
CT X1 DOWN) SAY.D)

********** LEFT down

6.  STM: ((EXPECT LEFT DOWN) (MADE (PRED)) (CRITERION DST) (DST BIG L
 BIG RIGHT) (WGT MORE RIGHT) (DST MORE LEFT))
  TRUE: E1: ((EXPECT) --> LOOK)
        ATTENDING - INPUT NEXT STIMULUS = >(see right down)

7.  STM: ((SEE RIGHT DOWN) (EXPECT LEFT DOWN) (MADE (PRED)) (CRITERIO
ST BIG LEFT) (WGT BIG RIGHT) (WGT MORE RIGHT) (DST MORE LEFT))
      CONFLICT.SET: (E1 E3)
  TRUE: E3: ((EXPECT X1 X2) (SEE X1 X2) ABS (SEE) --> (DID **) (SEE =
(RESULT WRONG))

10.  STM: ((RESULT WRONG) (DID (EXPECT LEFT DOWN)) (SAW RIGHT DOWN) (
D)) (CRITERION DST) (DST BIG LEFT) (WGT BIG RIGHT) (WGT MORE RIGHT) (
LEFT))
  TRUE: SW1: ((RESULT WRONG) (CRITERION DST) --> (OLD **) (DST ===> W

12.  STM: ((OLD (RESULT WRONG)) (CRITERION WGT) (DID (EXPECT LEFT DOW
RIGHT DOWN) (MADE (PRED)) (DST BIG LEFT) (WGT BIG RIGHT) (WGT MORE RI
 MORE LEFT))
```

```
>;now do problem 6. Keep criterion

TE: ((0102/2010))

0.  STM: ((PRED) (CRITERION WGT))
      CONFLICT.SET: (P8)
   TRUE: P8: ((PRED) (D1) ABS --> ATTEND)
         ATTENDING - INPUT NEXT STIMULUS = >(dst same)(wgt same)

1.  STM: ((WGT SAME) (DST SAME) (PRED) (CRITERION WGT)
)
   TRUE: P1: ((PRED) (WGT SAME) --> (MADE **) (EXPECT BALANCE EVEN) SA

********** balance

5.  STM: ((EXPECT BALANCE EVEN) (MADE (PRED)) (WGT SAME) (DST SAME) (
 WGT))
   TRUE: E1: ((EXPECT) --> LOOK)
         ATTENDING - INPUT NEXT STIMULUS = >(see balance even)

6.  STM: ((SEE BALANCE EVEN) (EXPECT BALANCE EVEN) (MADE (PRED)) (WGT
ST SAME) (CRITERION WGT))
      CONFLICT.SET: (E1 E2)
   TRUE: E2: ((EXPECT X1 X2) (SEE X1 X2) --> (DID **) (SEE ===> SAW) (
RRECT))

9.  STM: ((RESULT CORRECT) (DID (EXPECT BALANCE EVEN)) (SAW BALANCE E
E (PRED)) (WGT SAME) (DST SAME) (CRITERION WGT))
   TRUE: SW3: ((RESULT CORRECT) (CRITERION) --> (OLD **))

10.  STM: ((OLD (RESULT CORRECT)) (CRITERION WGT) (DID (EXPECT BALANC
(SAW BALANCE EVEN) (MADE (PRED)) (WGT SAME) (DST SAME))
>
```

```
>next problem 7 (0003/0020)

0. STM: ((PRED) (CRITERION WGT))
     CONFLICT.SET: (P8)
  TRUE: P8: ((PRED) (D1) ABS --> ATTEND)
       ATTENDING - INPUT NEXT STIMULUS = >(wgt more left)(dst more r

1. STM: ((DST MORE RIGHT) (WGT MORE LEFT) (PRED) (CRITERION WGT) )
     CONFLICT.SET: (P2 P4)
  TRUE: P4: ((PRED) (WGT MORE) (DST MORE) --> FIND.BIG)
       ATTENDING - INPUT NEXT STIMULUS = >(dst big right)(wgt big le

2. STM: ((WGT BIG LEFT) (DST BIG RIGHT) (PRED) (WGT MORE LEFT) (DST
T) (CRITERION WGT))
     CONFLICT.SET: (P2 P4 P5 P6 P7)
     CONFLICT.SET: (P4 P5) AFTER SPECIAL.CASE.ORDER
     CONFLICT.SET: (P5) AFTER STM.ORDER
  TRUE: P5: ((PRED) (CRITERION D1) (D1 BIG X1) (D2 BIG X2) --> (MADE
CT X1 DOWN) SAY.D)

********** LEFT down

6. STM: ((EXPECT LEFT DOWN) (MADE (PRED)) (CRITERION WGT) (WGT BIG L
 BIG RIGHT) (WGT MORE LEFT) (DST MORE RIGHT))
  TRUE: E1: ((EXPECT) --> LOOK)
       ATTENDING - INPUT NEXT STIMULUS = >(see right down)

7. STM: ((SEE RIGHT DOWN) (EXPECT LEFT DOWN) (MADE (PRED)) (CRITERIO
GT BIG LEFT) (DST BIG RIGHT) (WGT MORE LEFT) (DST MORE RIGHT))
     CONFLICT.SET: (E3) AFTER SPECIAL.CASE.ORDER
  TRUE: E3: ((EXPECT X1 X2) (SEE X1 X2) ABS (SEE) --> (DID **) (SEE =
(RESULT WRONG))


10. STM: ((RESULT WRONG) (DID (EXPECT LEFT DOWN)) (SAW RIGHT DOWN) (
D)) (CRITERION WGT) (WGT BIG LEFT) (DST BIG RIGHT) (WGT MORE LEFT) (D
IGHT))
  TRUE: SW2: ((RESULT WRONG) (CRITERION WGT) --> (OLD **) (WGT ===> D

12. STM: ((OLD (RESULT WRONG)) (CRITERION DST) (DID (EXPECT LEFT DOW
RIGHT DOWN) (MADE (PRED)) (WGT BIG LEFT) (DST BIG RIGHT) (WGT MORE LE
MORE RIGHT))
```

```
>;prob 8  (0100/0200)  notice, this has big dst, but not big wgt
>

0.  STM: ((PRED) (CRITERION DST))
  TRUE: P8: ((PRED) (D1) ABS --> ATTEND)
        ATTENDING - INPUT NEXT STIMULUS = >(wgt more right)(dst more

1.  STM: ((DST MORE LEFT) (WGT MORE RIGHT) (PRED) (CRITERION DST) )
      CONFLICT.SET: (P2 P4)
  TRUE: P4: ((PRED) (WGT MORE) (DST MORE) --> FIND.BIG)
        ATTENDING - INPUT NEXT STIMULUS = >(dst big left)

2.  STM: ((DST BIG LEFT) (PRED) (WGT MORE RIGHT) (DST MORE LEFT) (CRI
T))
      CONFLICT.SET: (P2 P4 P7)
      CONFLICT.SET: (P4 P7) AFTER SPECIAL.CASE.ORDER
      CONFLICT.SET: (P7) AFTER STM.ORDER
  TRUE: P7: ((PRED) (DST BIG X1) --> (MADE **) (EXPECT X1 DOWN) SAY.D

********** LEFT down

6.  STM: ((EXPECT LEFT DOWN) (MADE (PRED)) (DST BIG LEFT) (WGT MORE R
T MORE LEFT) (CRITERION DST))
  TRUE: E1: ((EXPECT) --> LOOK)
        ATTENDING - INPUT NEXT STIMULUS = >(see right down)

7.  STM: ((SEE RIGHT DOWN) (EXPECT LEFT DOWN) (MADE (PRED)) (DST BIG
T MORE RIGHT) (DST MORE LEFT) (CRITERION DST))
      CONFLICT.SET: (E1 E3)
  TRUE: E3: ((EXPECT X1 X2) (SEE X1 X2) ABS (SEE) --> (DID **) (SEE =
(RESULT WRONG))

10.  STM: ((RESULT WRONG) (DID (EXPECT LEFT DOWN)) (SAW RIGHT DOWN) (
D)) (DST BIG LEFT) (WGT MORE RIGHT) (DST MORE LEFT) (CRITERION DST))
  TRUE: SW1: ((RESULT WRONG) (CRITERION DST) --> (OLD **) (DST ===> W

12.  STM: ((OLD (RESULT WRONG)) (CRITERION WGT) (DID (EXPECT LEFT DOW
RIGHT DOWN) (MADE (PRED)) (DST BIG LEFT) (WGT MORE RIGHT) (DST MORE L
NIL)
```